

Does (asymptotically safe) quantum gravity
have to be a TOE?

Workshop on strongly-interacting field theories,
TPI Jena
Nov. 7, 2015

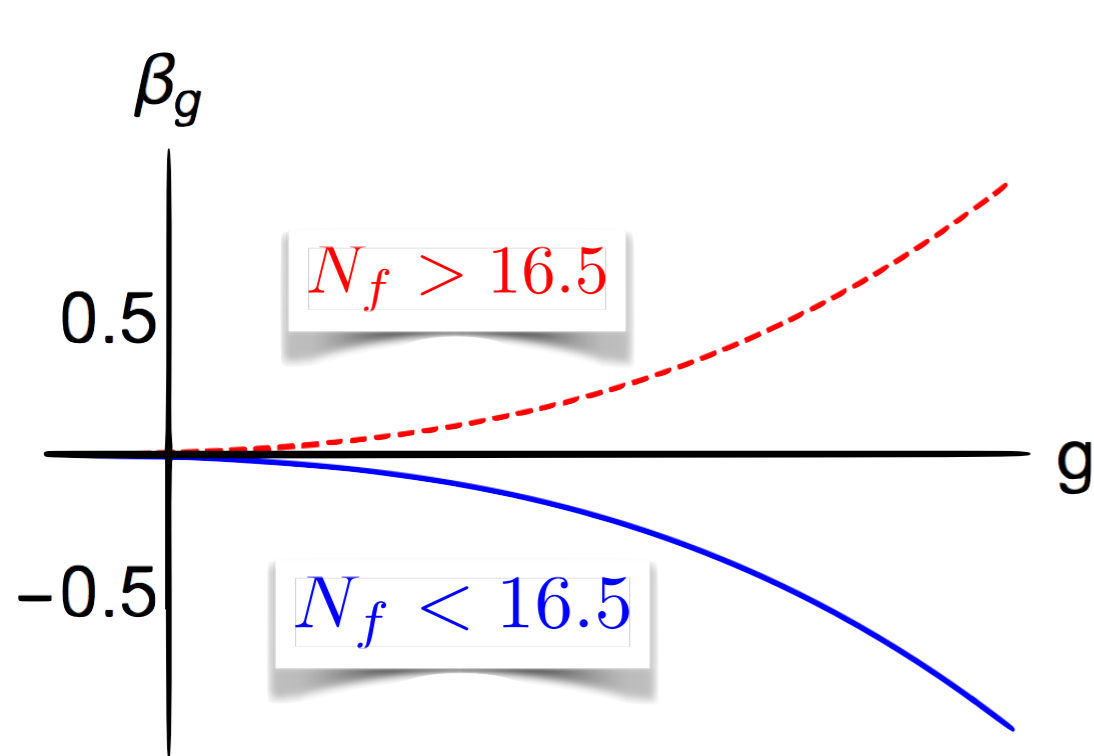
Astrid Eichhorn, Imperial College, London

Quantum spacetime and matter?

Is it “safe” to ignore matter degrees of freedom while exploring the quantum structure of spacetime?

Quantum spacetime and matter?

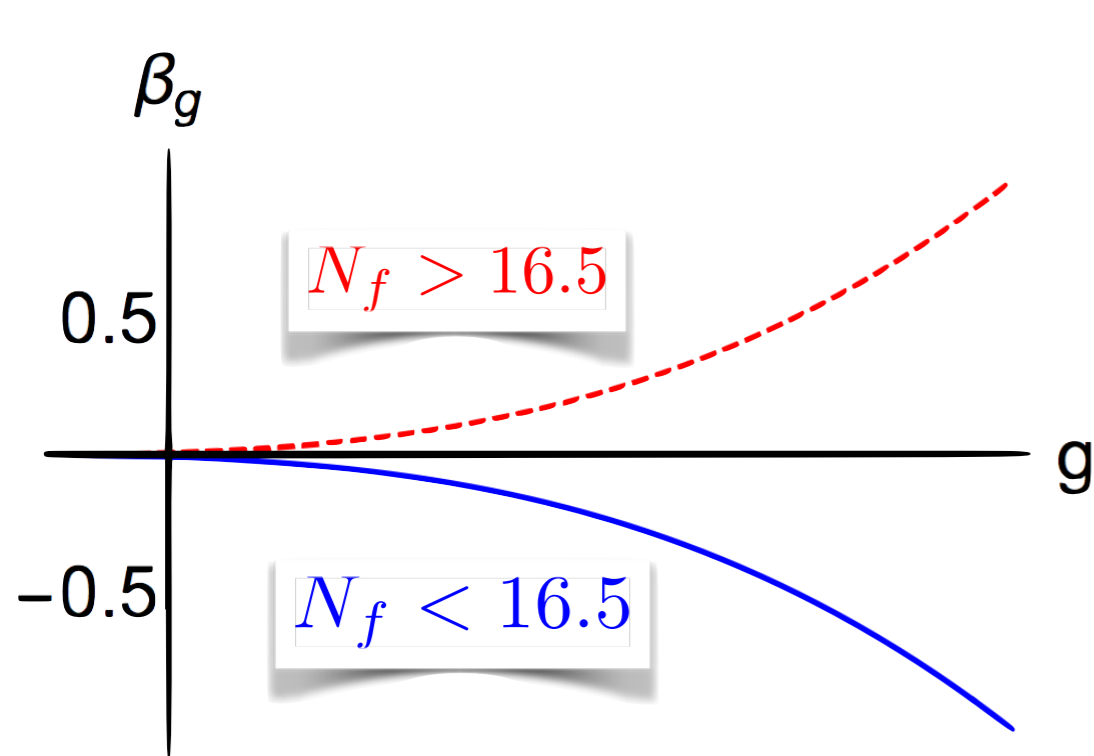
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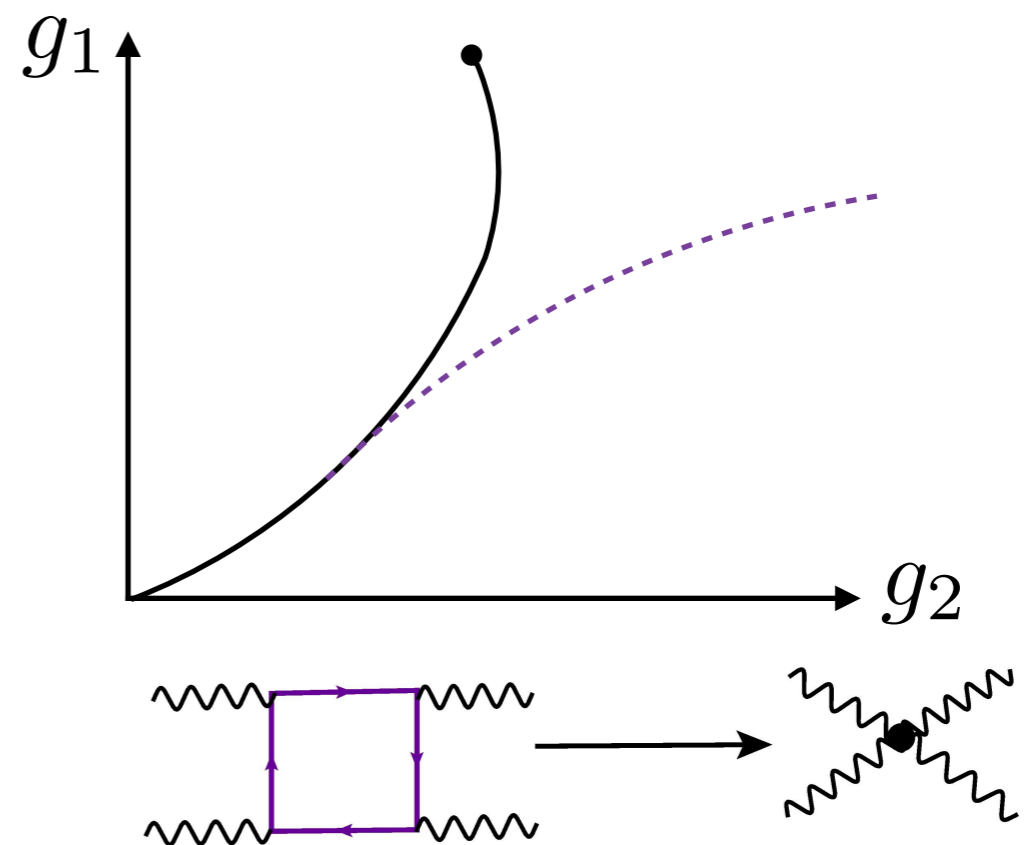
Asymptotic freedom in Yang-Mills theories does not exist for arbitrary number of matter fields

Quantum spacetime and matter?

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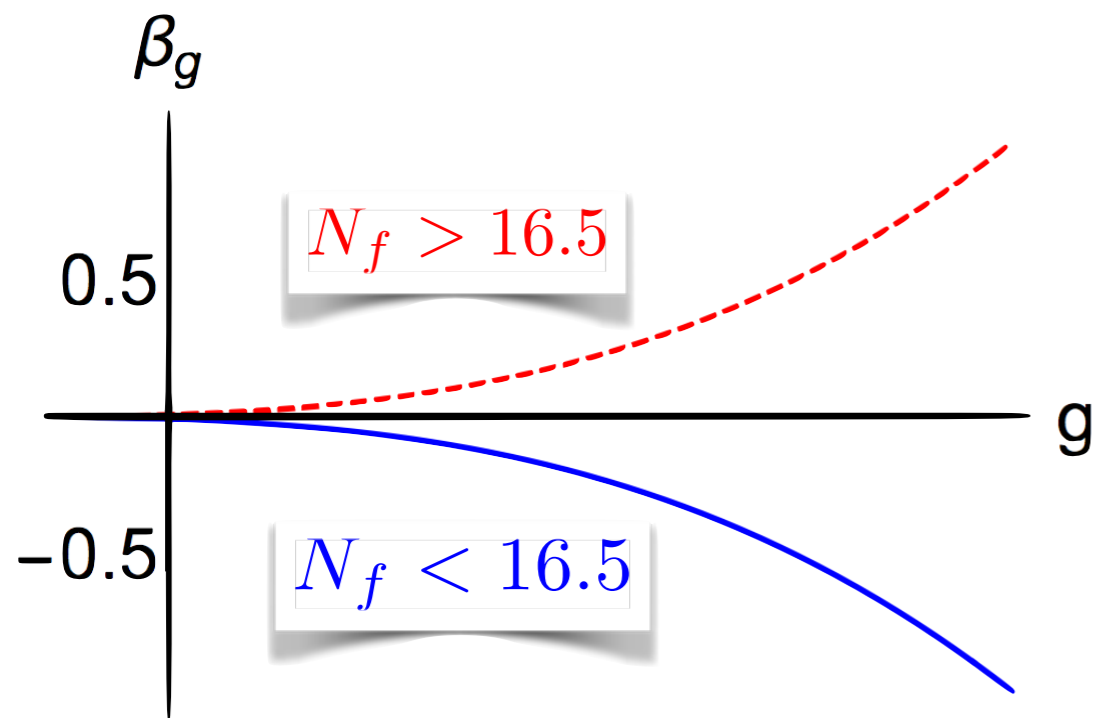


Asymptotic freedom in Yang-Mills theories does not exist for arbitrary number of matter fields

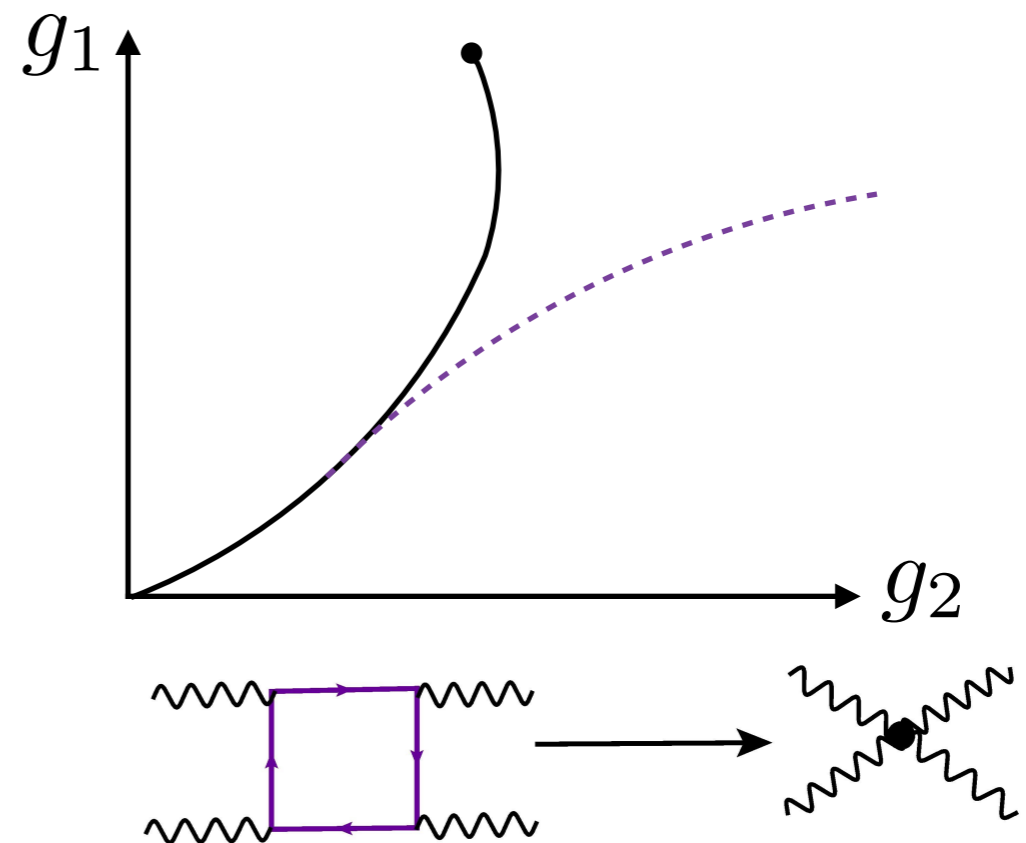


Quantum spacetime and matter?

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Asymptotic freedom in Yang-Mills theories does not exist for arbitrary number of matter fields

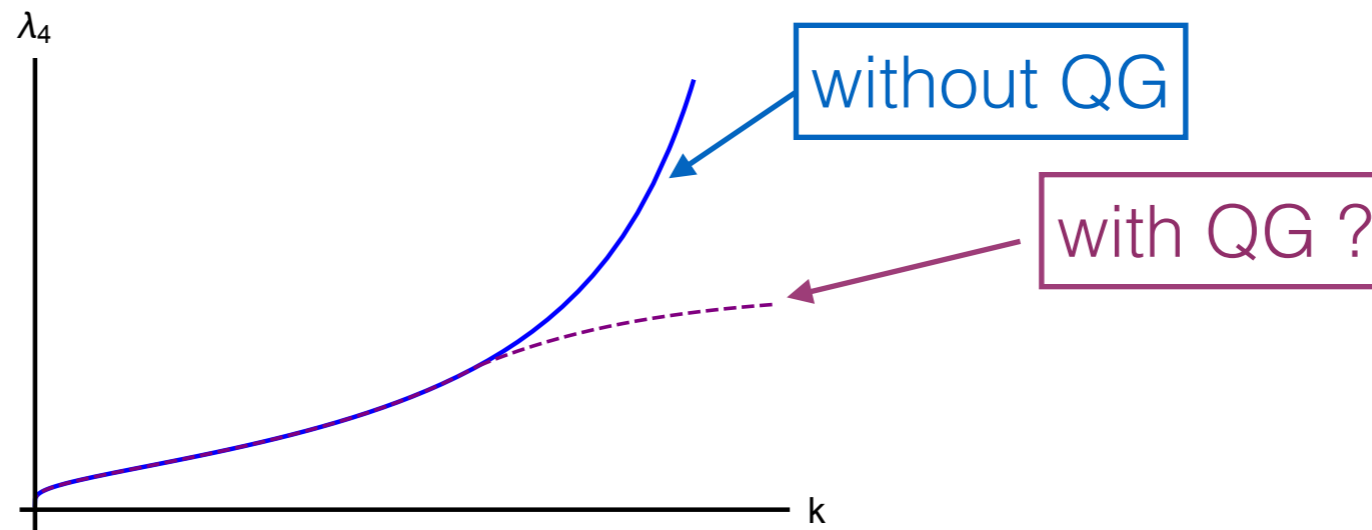


In sum-over-histories setting for QG, matter fluctuations will generically change microscopic gravitational dynamics

Quantum spacetime and matter?

Open problems in the Standard Model:

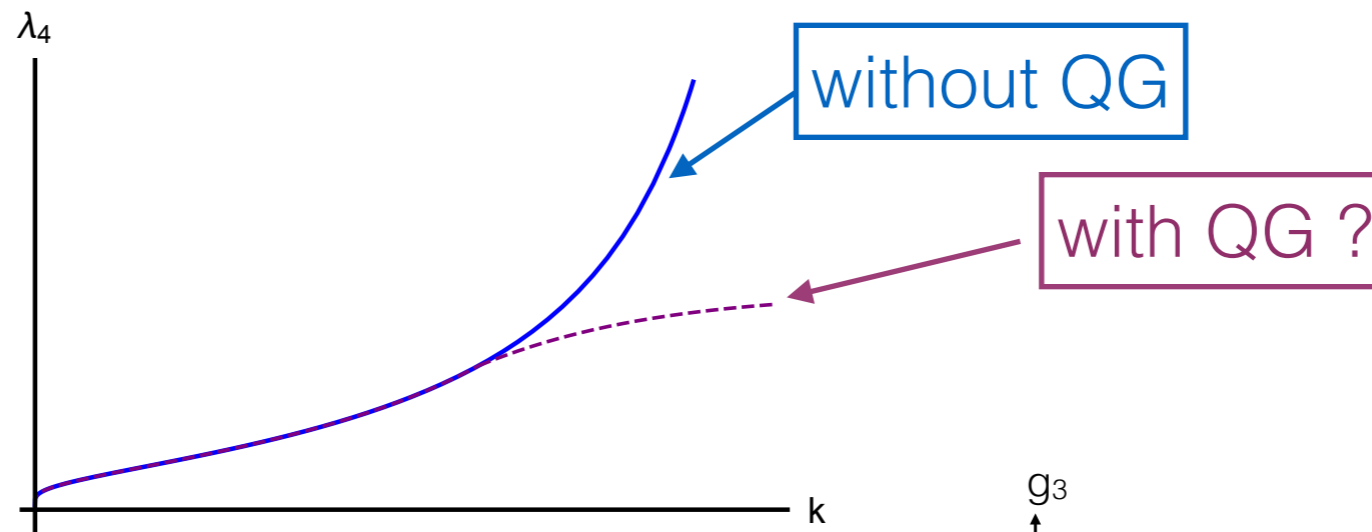
- triviality problem in $U(1)_Y$ and Higgs quartic coupling



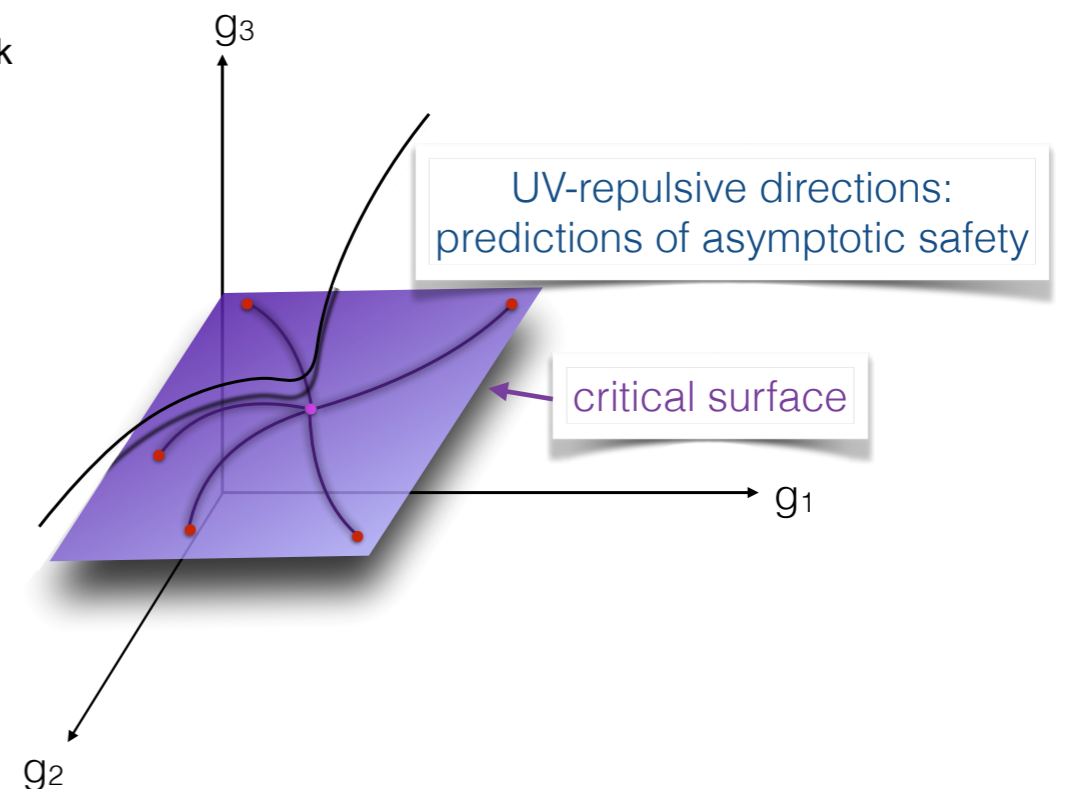
Quantum spacetime and matter?

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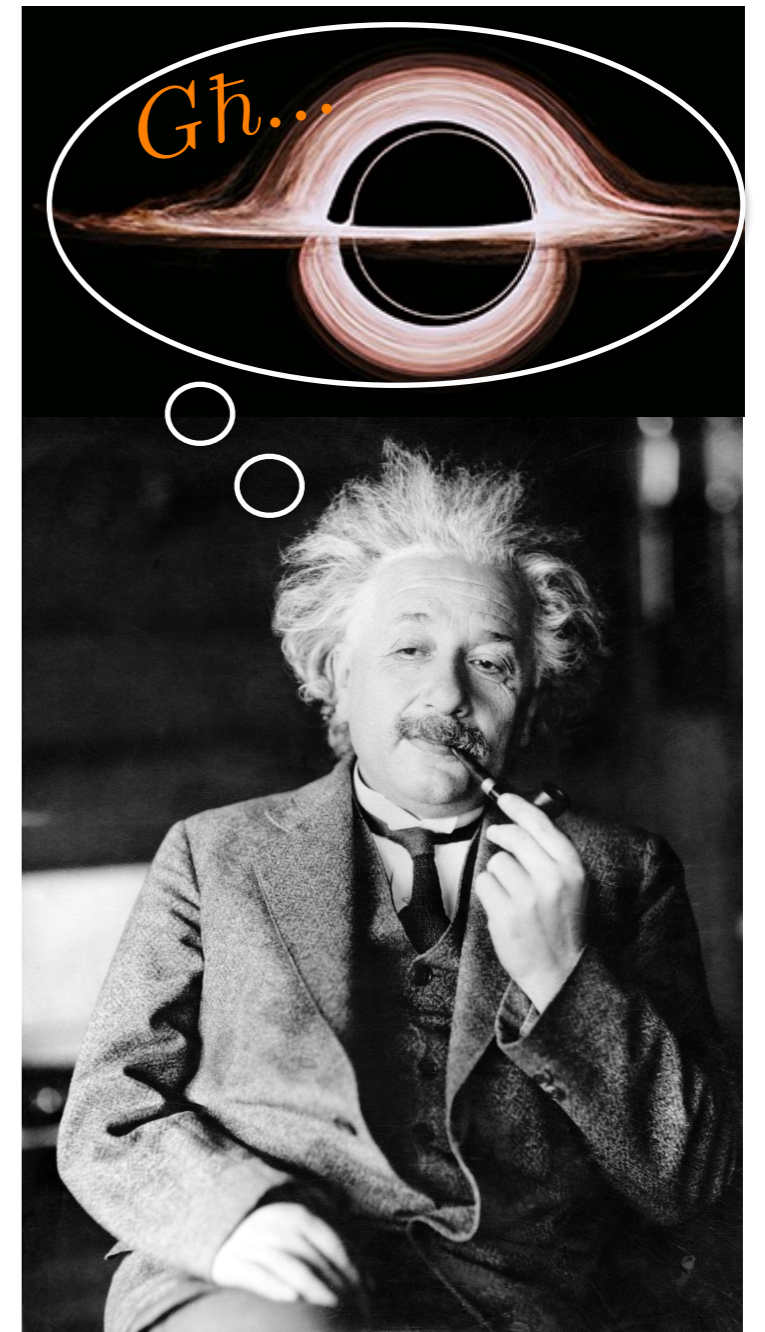
- triviality problem in $U(1)_Y$ and Higgs quartic coupling



- predictions of free parameters of the Standard Model (e.g. Yukawa couplings) possible?



Including matter:
Possibilities to test quantum gravity observationally?



Including matter: Possibilities to test quantum gravity observationally?

quantum gravity model has to admit
existence and properties of observed matter

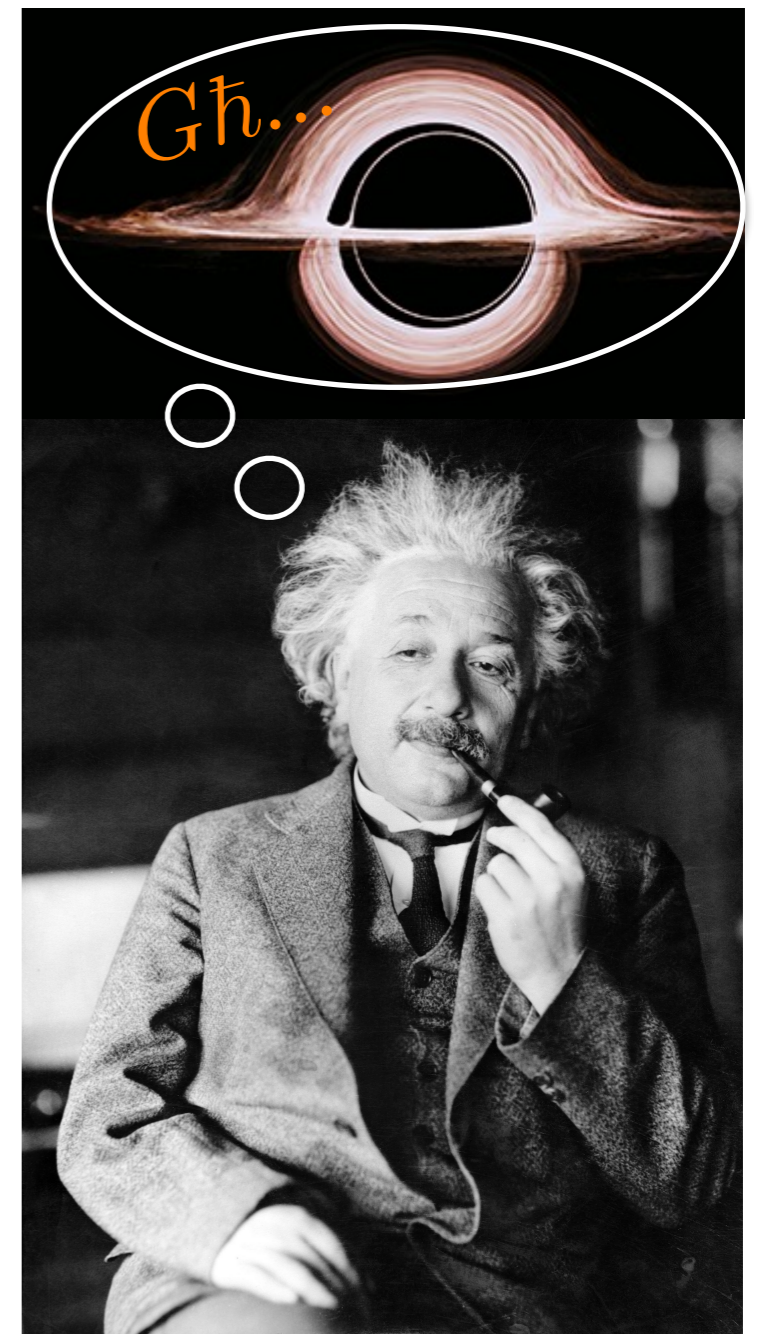
Example: chiral (i.e. light) fermions

within truncation: compatible
with asymptotically safe gravity

A.E., H. Gies, '11

no clear indications in
Loop Quantum Gravity

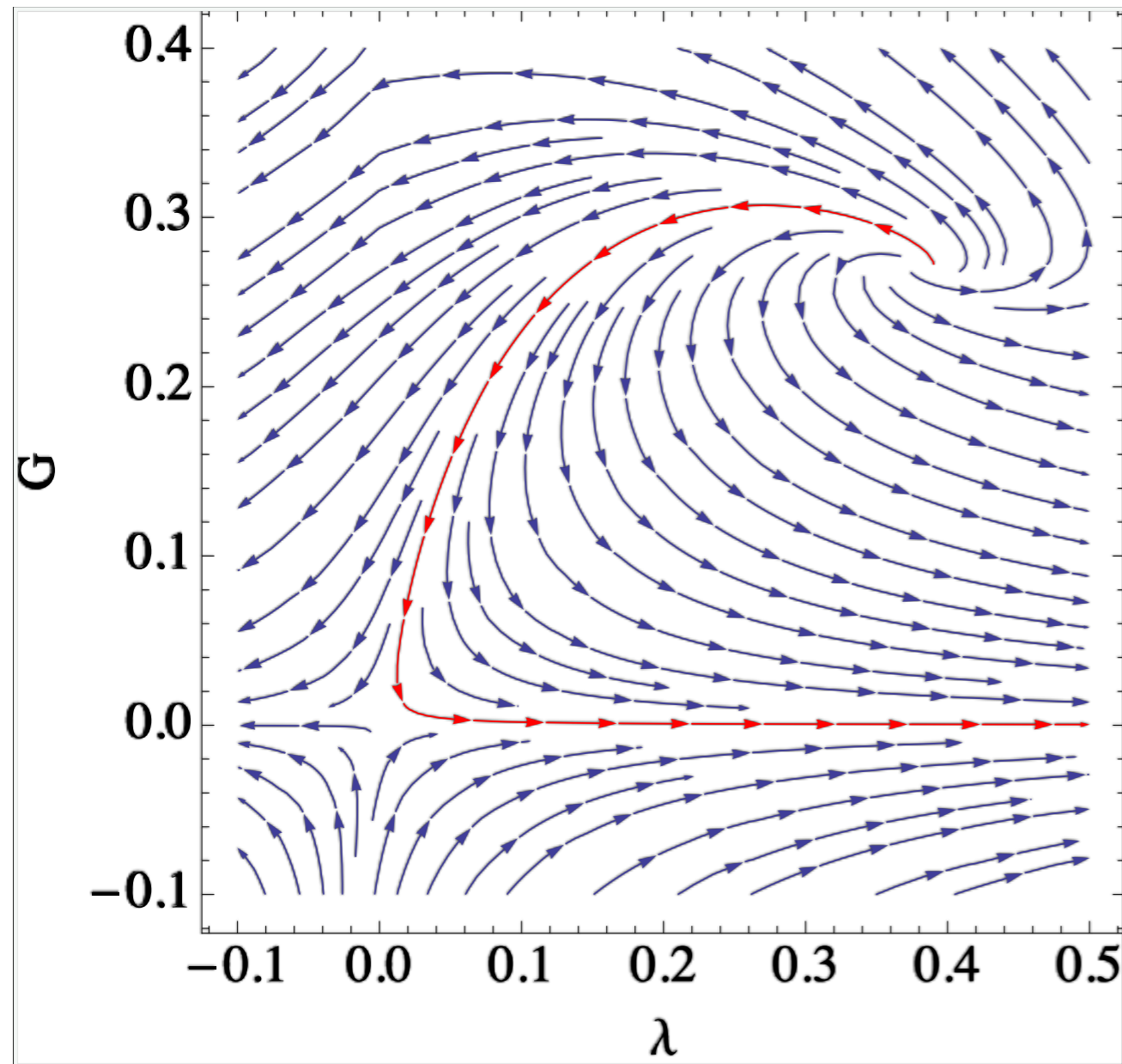
Barnett, Smolin, '15;
Gambini, Pullin, '15



Evidence for asymptotic safety in gravity

$$\Gamma_k = -\frac{1}{16\pi G_N(k)} \int d^4x \sqrt{g} (R - 2\bar{\lambda}(k))$$

$$G(k) = G_N k^2, \quad \lambda(k) = \bar{\lambda}(k)/k^2$$



interacting fixed point
with ~ 3 (?) relevant directions

extended truncations:

- gauge fixing & ghosts

Groh, Saueressig, '10; Eichhorn, Gies, '10; Eichhorn, '13

- distinction of background & fluctuation couplings

Manrique, Reuter, Saueressig, '11;
Christiansen, Litim, Pawłowski, Rodigast, '14;
Codello, D'Odorico, Pagani, '14; Becker, Reuter, '14, '15;
Christiansen, Knorr, Meibohm, Pawłowski, Reichert, '15

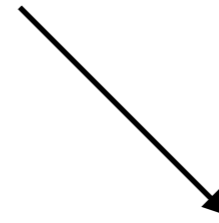
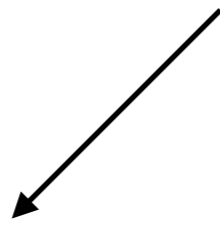
- higher curvature terms

$f(R)$ Reuter, Lauscher, '02; Codello, Percacci, Rahmede, '09;
Benedetti, Caravelli, '12; Dietz, Morris, '12;
Demmel, Saueressig, Zanusso, '15

Reuter, '96; Reuter, Saueressig '01, Litim, '03

$R^2, R_{\mu\nu}R^{\mu\nu}$ Benedetti, Machado, Saueressig, '09

Matter degrees of freedom



fundamental
→ need to
include in
microscopic model

effective
“matter from spacetime”:
(Kaluza Klein;
scalars from $f(R)$)

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in asymptotic safety:
standard QFT framework, so matter fields ‘simple’

Possible structure of a fixed point for gravity + matter

Possible structure of a fixed point for gravity + matter

use simple(r) example of interacting fixed point:

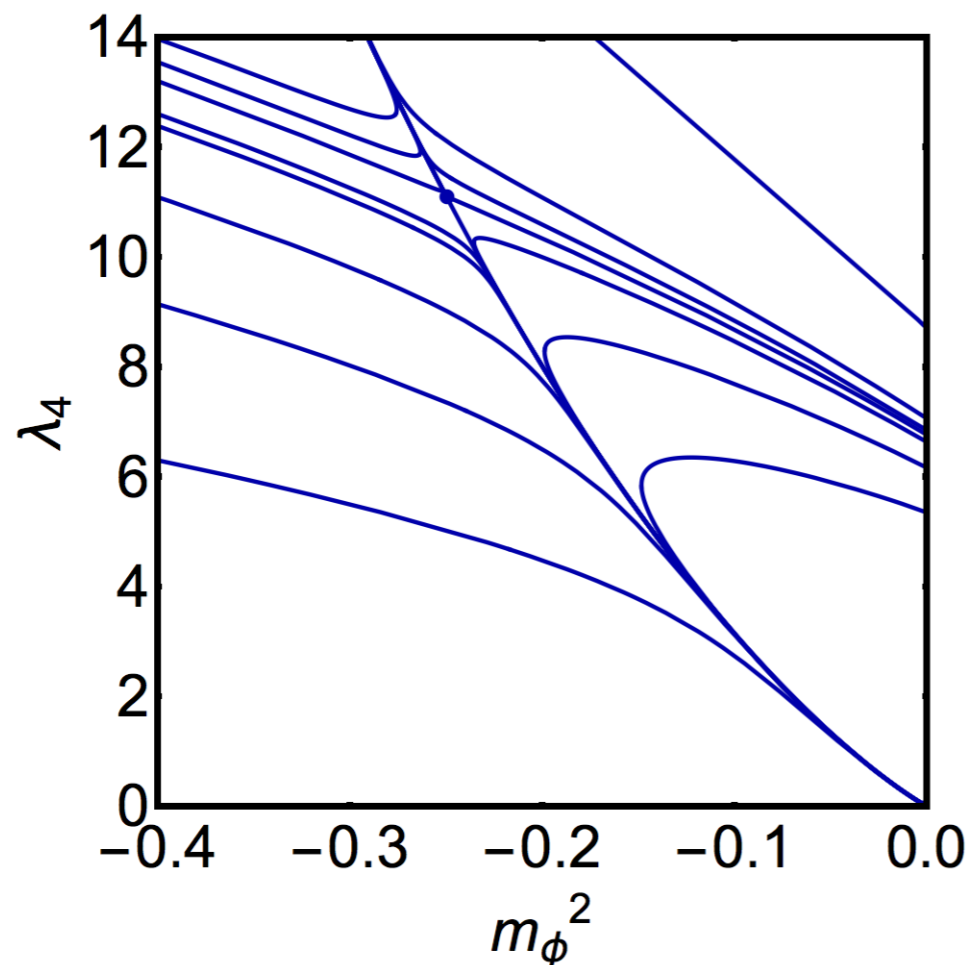
Wilson-Fisher fixed point & generalisations in $O(N)$ symmetric
3d scalar model

Possible structure of a fixed point for gravity + matter

use simple(r) example of interacting fixed point:

Wilson-Fisher fixed point & generalisations in $O(N)$ symmetric 3d scalar model

$$V(\phi^2) = \frac{m_\phi^2}{2} \phi_i \phi^i + \frac{\lambda_4}{8} (\phi_i \phi^i)^2 \quad i = 1, \dots, N$$

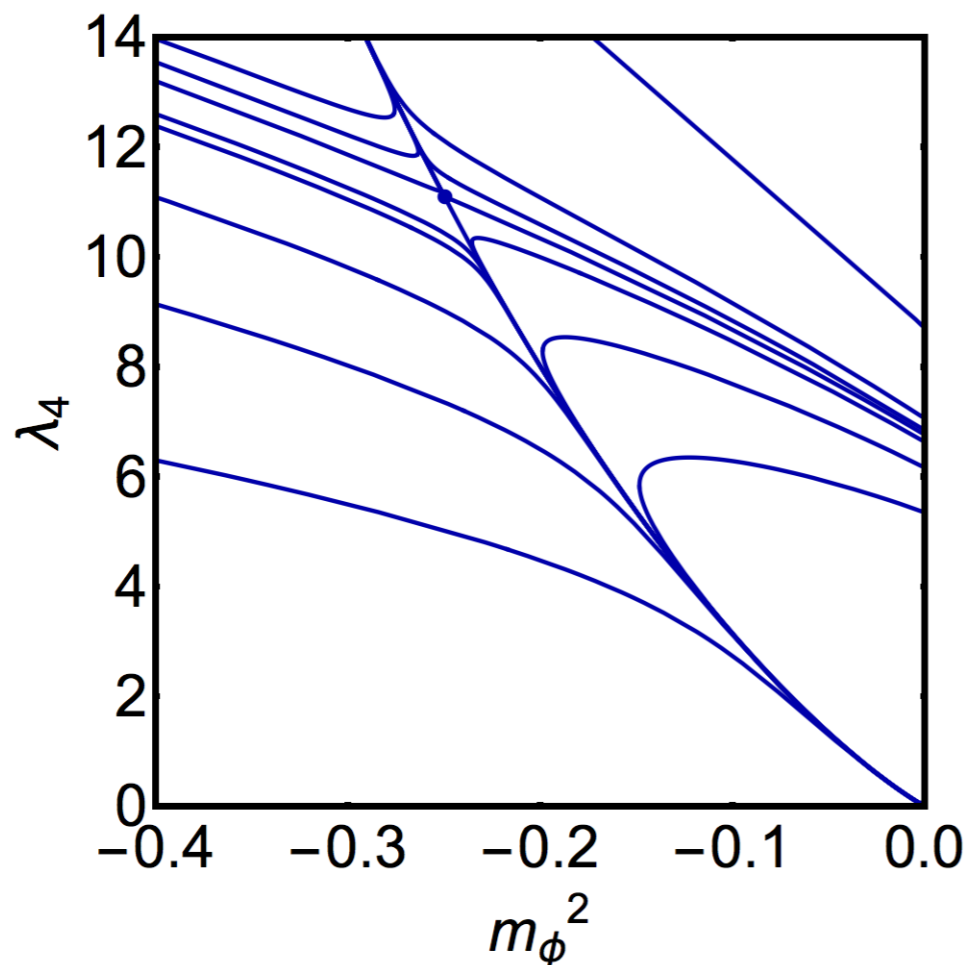


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add a second $O(M)$ scalar:

$$V_{\text{int}} = \frac{\lambda_{2,2}}{4} \phi_i \phi^i \chi_j \chi^j$$

What are possible fixed points?

A.E., D. Mesterházy, M. Scherer, '13, '14
A.E., T. Helfer, D. Mesterházy, M. Scherer, '15

Possible structure of a fixed point for gravity + matter

use simple(r) example of interacting fixed point:

Wilson-Fisher fixed point & generalisations in $O(N)$ symmetric 3d scalar model

| | λ_{ϕ^4} | λ_{χ^4} | $\lambda_{2,2}$ | |
|---------------|--------------------|--------------------|-----------------|--|
| semi-Gaussian | $\neq 0$ | $= 0$ | $= 0$ | |
| | | | | |
| | | | | |
| | | | | |

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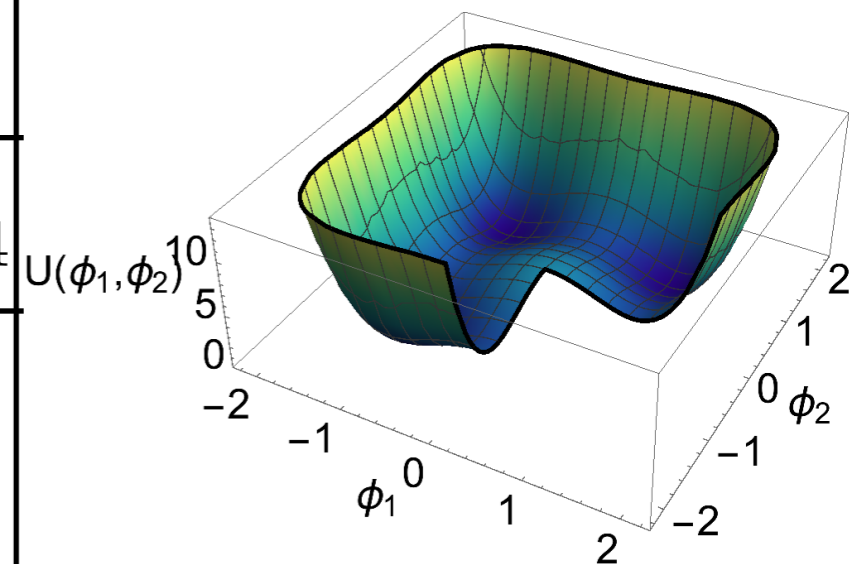
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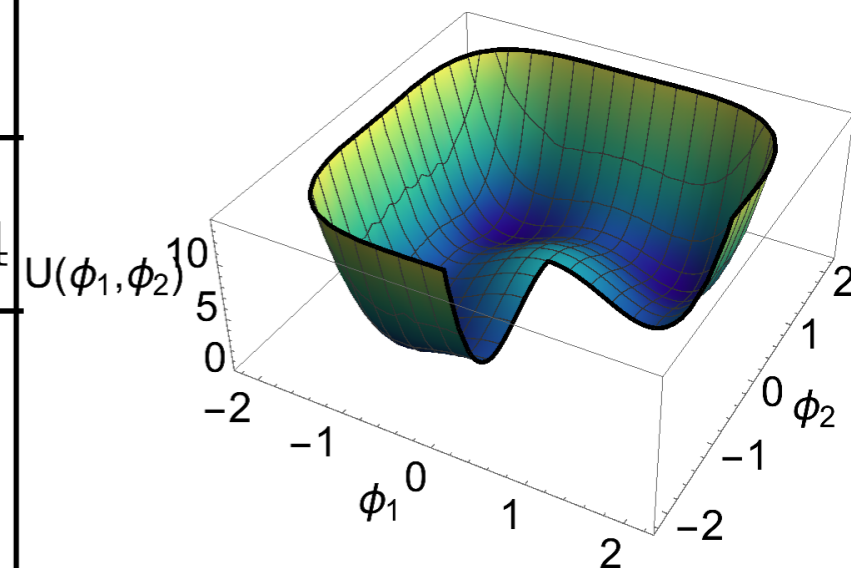


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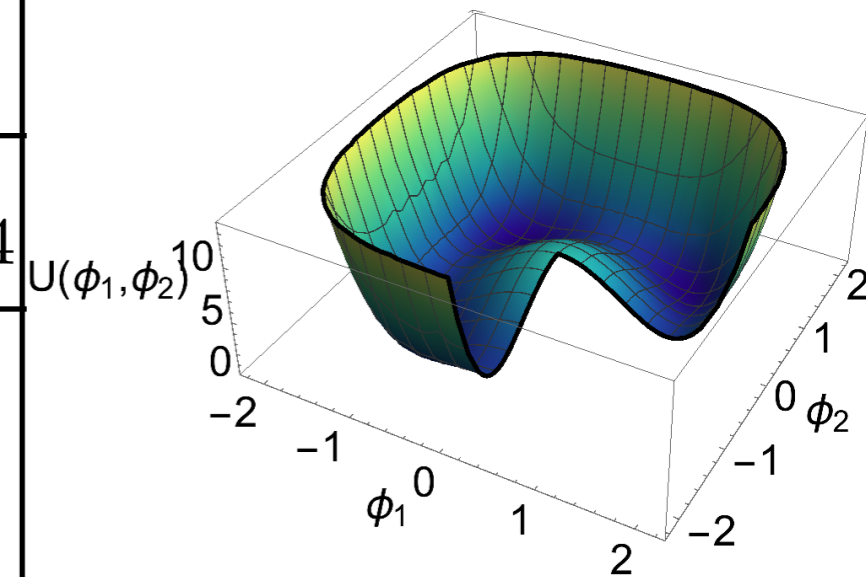


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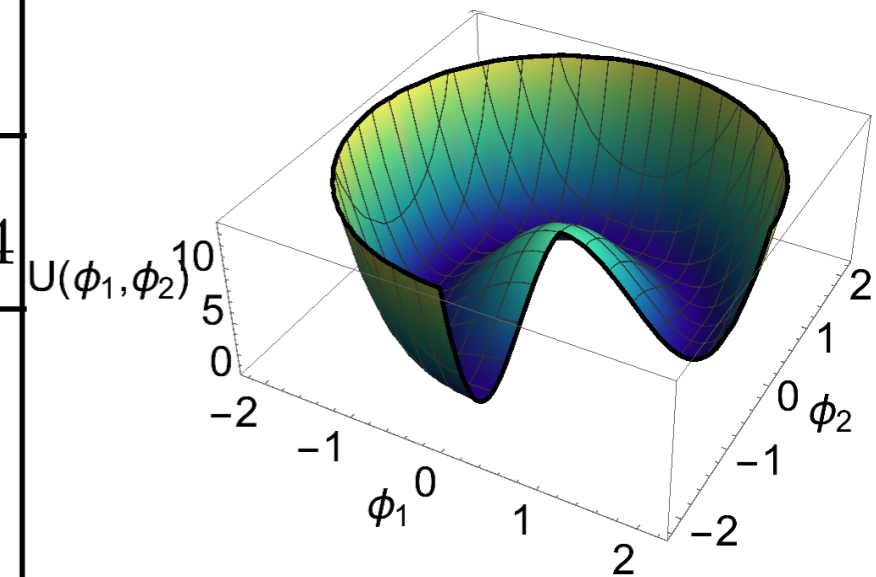


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| biconical | $\neq 0$ | $\neq 0$ | $\neq 0$ | → induced by nontrivial interactions between both sectors |

Nelson, Kosterlitz, Fisher '74;
 Calabrese, Pelissetto, Vicari '03;
 Folk, Holovatch, Moser '08;
 Eichhorn, Mesterházy, Scherer '13

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Standard Model
(most probably)
not UV complete
by itself

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supergravity?

Possible structure of a fixed point for gravity + matter

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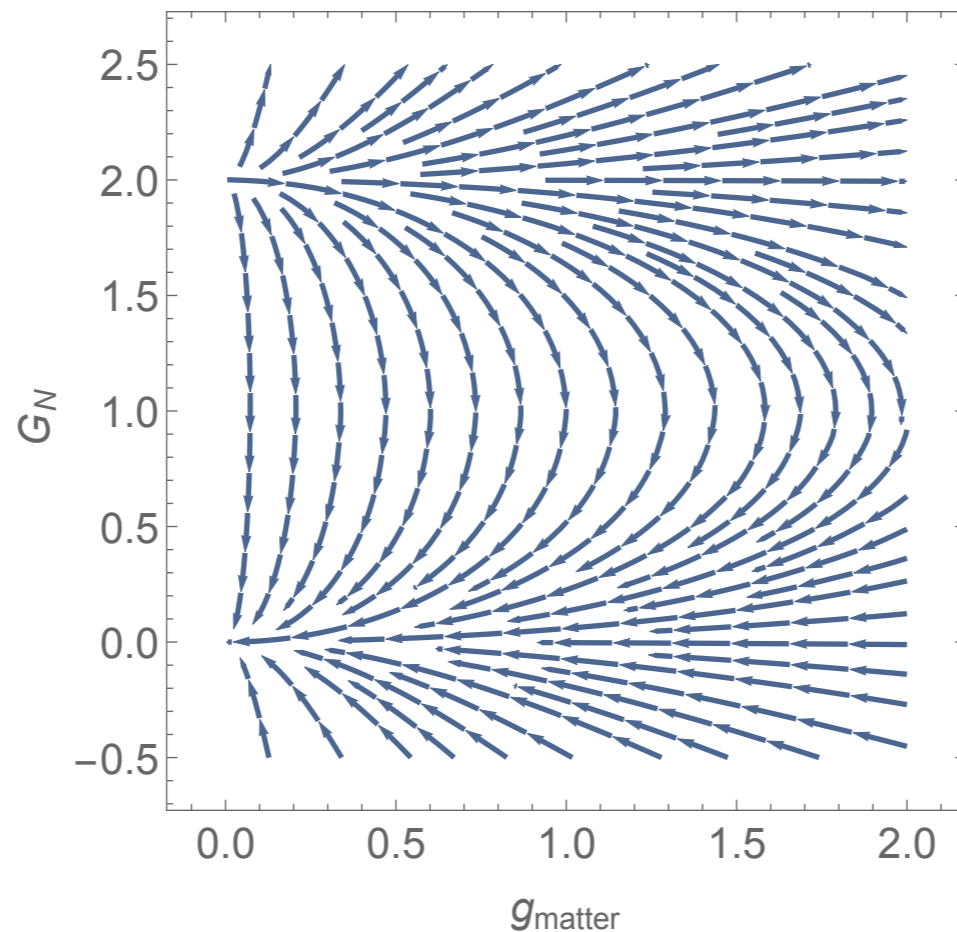
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Possible structure of a fixed point for gravity + matter

Gaussian matter fixed point:
Gravitational couplings finite; matter couplings vanish

$$\int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \quad i \int d^d x \sqrt{g} \bar{\psi} \not{\nabla} \psi$$



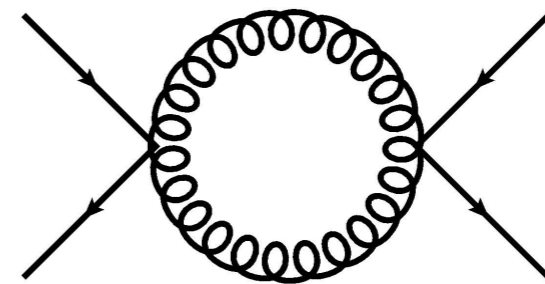
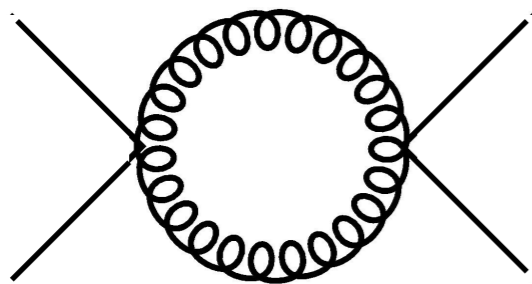
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$$i \int d^d x \sqrt{g} \bar{\psi} \not{\nabla} \psi$$



$$\rho \int d^4 \sqrt{g} g^{\mu\nu} (\partial_\mu \phi \partial_\nu \phi) g^{\kappa\lambda} (\partial_\kappa \phi \partial_\lambda \phi)$$

$$\lambda_\pm \int d^4 \sqrt{g} (\bar{\psi} \gamma_\mu \psi \bar{\psi} \gamma^\mu \psi \pm \bar{\psi} \gamma_\mu \gamma_5 \psi \bar{\psi} \gamma^\mu \gamma_5 \psi)$$

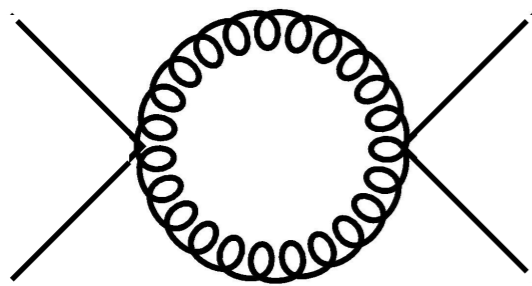
Structure of a fixed point for gravity + matter

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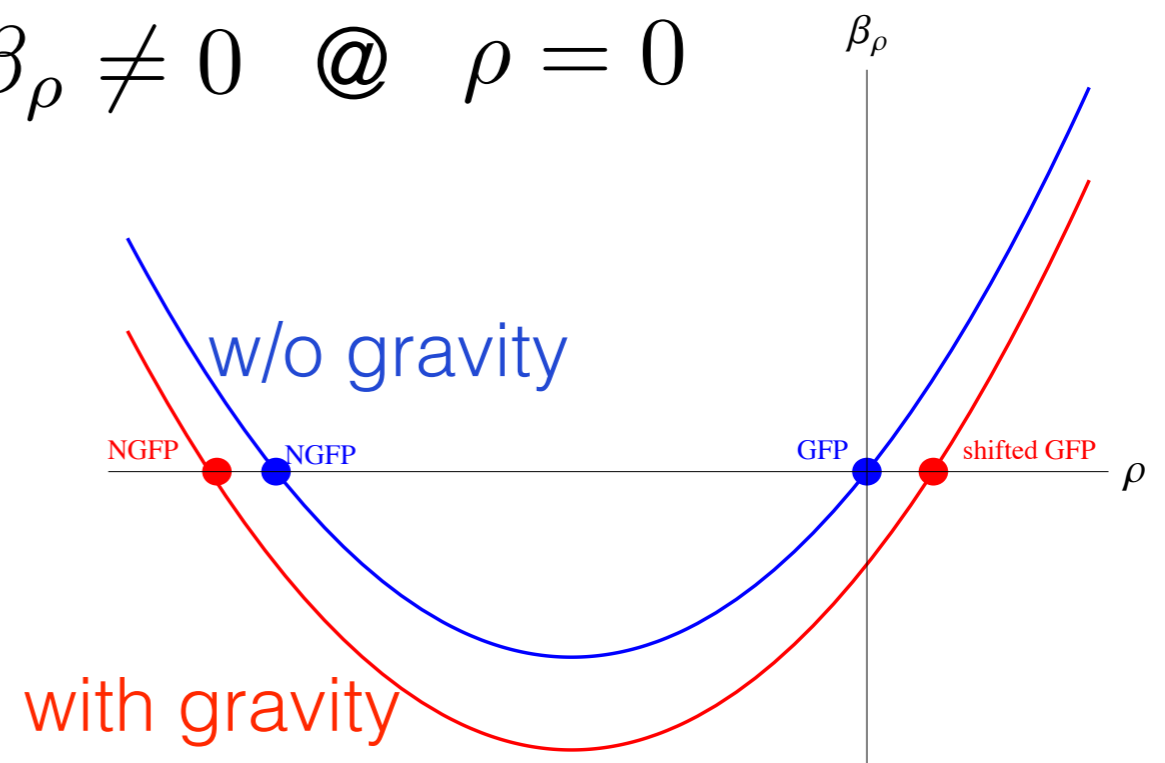
$$\int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$$

$$\beta_\rho = \dots + \#G^2$$

$$\Rightarrow \beta_\rho \neq 0 \text{ @ } \rho = 0$$



$$\rho \int d^4 \sqrt{g} g^{\mu\nu} (\partial_\mu \phi \partial_\nu \phi) g^{\kappa\lambda} (\partial_\kappa \phi \partial_\lambda \phi)$$



Structure of a fixed point for gravity + matter

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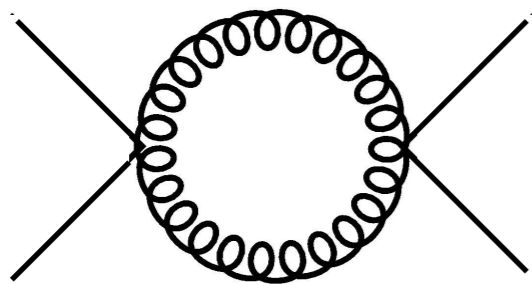
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$$\Rightarrow \lambda_{\phi^4} \neq 0$$



$$\rho \int d^4 \sqrt{g} g^{\mu\nu} (\partial_\mu \phi \partial_\nu \phi) g^{\kappa\lambda} (\partial_\kappa \phi \partial_\lambda \phi)$$

A.E., '12

Gaussian matter fixed point appears to be truncation artefact

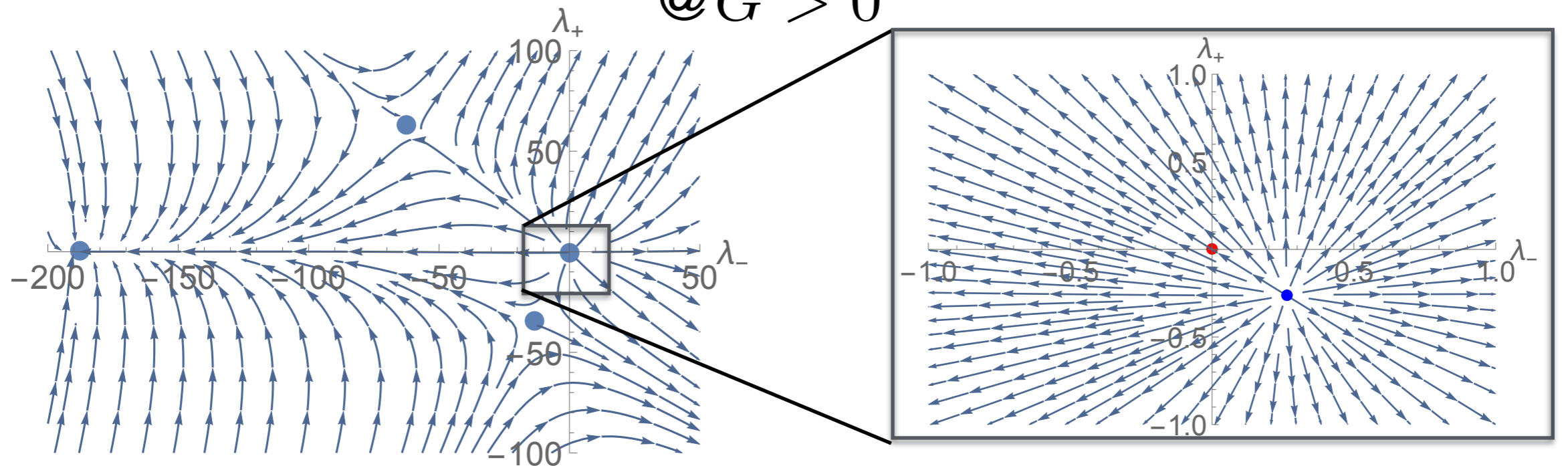
truncations beyond LPA required

Structure of a fixed point for gravity + matter

Gaussian matter fixed point:
 Gravitational couplings finite; matter couplings vanish

$$i \int d^d x \sqrt{g} \bar{\psi} \not{\nabla} \psi \quad \rightarrow \quad \lambda_{\pm} \int d^4 \sqrt{g} (\bar{\psi} \gamma_{\mu} \psi \bar{\psi} \gamma^{\mu} \psi \pm \bar{\psi} \gamma_{\mu} \gamma_5 \psi \bar{\psi} \gamma^{\mu} \gamma_5 \psi)$$

@ $G > 0$



A.E., H. Gies, '11

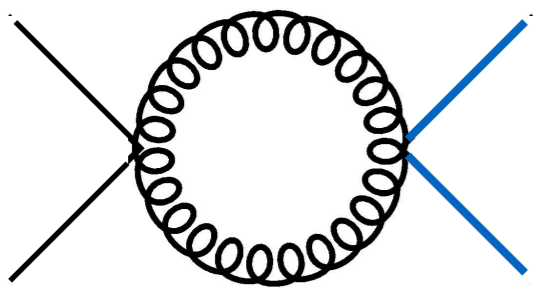
gravity-fermion fixed point
 is interacting

Structure of a fixed point for gravity + matter

Phenomenological consequence:

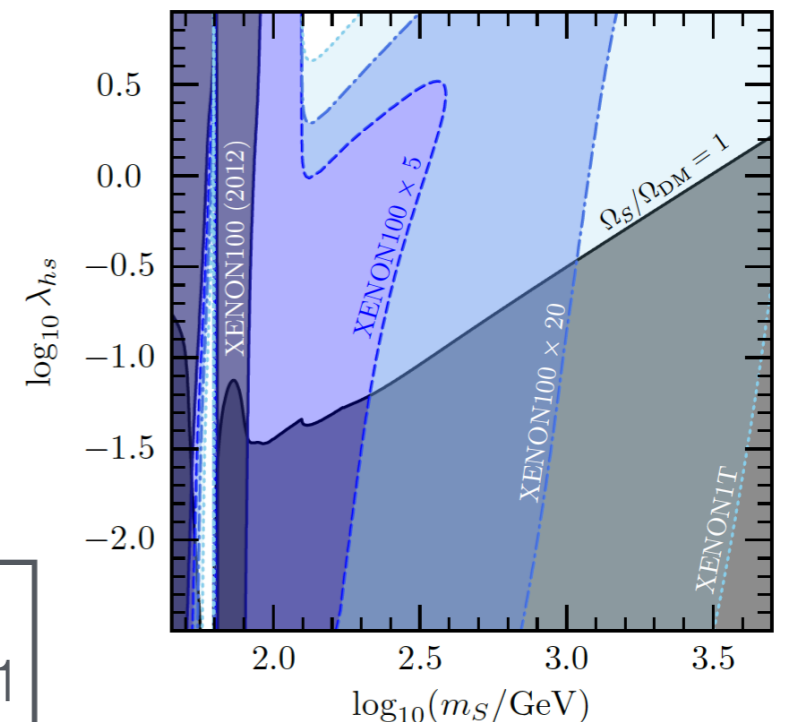
If dark matter is scalar, Higgs portal coupling in asymptotic safety is finite

$$\int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi + \int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \chi \partial_\nu \chi$$



$$\rightarrow \lambda_{2,2} \phi^2 \chi^2 \neq 0$$


Silveira, Zee '85; McDonald '94;
Burgess, Pospelov, ter Veldhuis '01



Cline, Scott, Kainulainen,
Weniger, '13

Open question: Can we predict Higgs-portal coupling from asymptotic safety?

Gravitational effects on the Yukawa sector

$$\int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \qquad i \int d^d x \sqrt{g} \bar{\psi} \not{\nabla} \psi$$

$$X \int d^d x \sqrt{g} (\bar{\psi} \gamma^\mu \psi) (D_\mu g^{\kappa\lambda} \partial_\kappa \phi \partial_\lambda \phi)$$

Poster: A. Held

Gravitational effects on the Yukawa sector

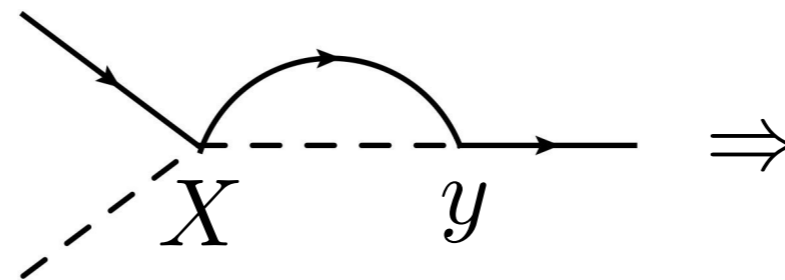
$$\int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \qquad i \int d^d x \sqrt{g} \bar{\psi} \not{\nabla} \psi$$

\swarrow \swarrow
 $X \int d^d x \sqrt{g} (\bar{\psi} \gamma^\mu \psi) (D_\mu g^{\kappa\lambda} \partial_\kappa \phi \partial_\lambda \phi)$

$$X_* \neq 0$$

Poster: A. Held

$$y \int d^d x \sqrt{x} \bar{\psi} \psi \phi$$



\Rightarrow

additional contribution
to critical exponent
from
[Zanusso, Zambelli, Vacca,
Percacci, '09;
Zanusso, Vacca, '10]

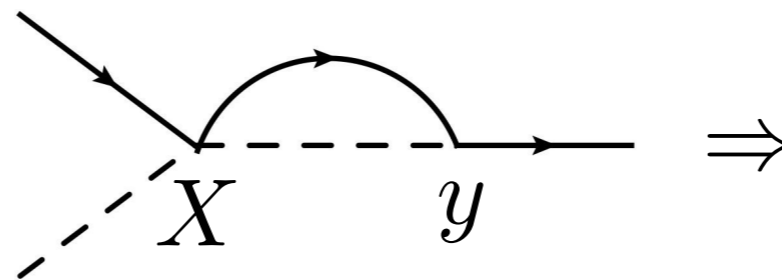
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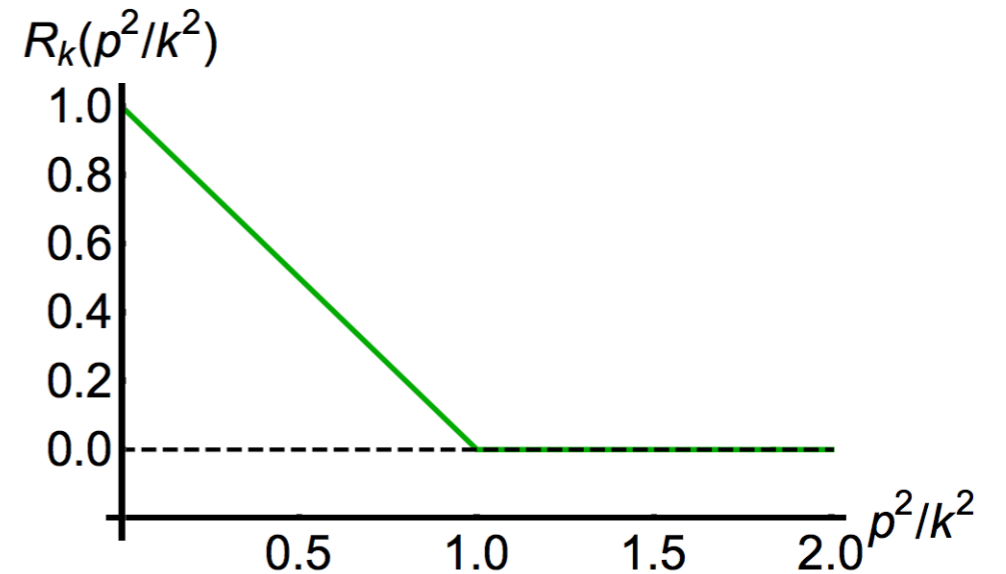
Can asymptotic safety predict the structure
of the Yukawa sector? ...stay tuned...

Setting a scale in quantum gravity?

Setting a scale in quantum gravity?

$$\int \mathcal{D}\varphi e^{-S[\varphi] - \int_p \varphi(p) R_k(p^2) \varphi(-p)}$$

Wetterich '93; Morris '94



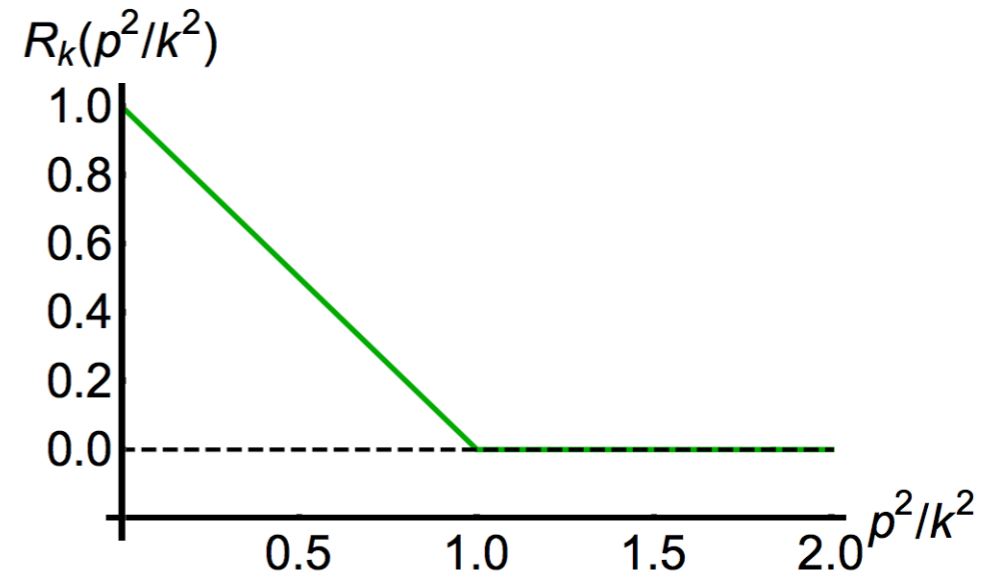
on a flat background: $\varphi(x) = \int_p \tilde{\varphi}(p) e^{ip \cdot x}$

on a curved background $\bar{g}_{\mu\nu}$: $p^2 \rightarrow -\bar{D}^2$

Setting a scale in quantum gravity?

$$\int \mathcal{D}\varphi e^{-S[\varphi] - \int_p \varphi(p) R_k(p^2) \varphi(-p)}$$

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on a flat background: $\varphi(x) = \int_p \tilde{\varphi}(p) e^{ip \cdot x}$

on a curved background $\bar{g}_{\mu\nu}$: $p^2 \rightarrow -\bar{D}^2$

in quantum gravity: $g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}$ or $g_{\mu\nu} = \bar{g}_{\mu\kappa} \left(e^{h \cdot} \right)^\kappa_\nu$

path integral:

$$\int \mathcal{D}g_{\mu\nu} e^{-S[g_{\mu\nu}]} \rightarrow \int \mathcal{D}h_{\mu\nu} e^{-S[\bar{g}_{\mu\nu} + h_{\mu\nu}]}$$

scale setting:

$$h_{\mu\nu} R_k^{\mu\nu\kappa\lambda}(-\bar{D}^2) h_{\kappa\lambda}$$

Setting a scale in quantum gravity?

in quantum gravity: $g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}$ or $g_{\mu\nu} = \bar{g}_{\mu\kappa} \left(e^{h \cdot} \right)_{\nu}^{\kappa}$

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$$h_{\mu\nu} R_{\kappa}^{\mu\nu\kappa\lambda} (-\bar{D}^2) h_{\kappa\lambda}$$

Setting a scale in quantum gravity?

in quantum gravity: $g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}$ or $g_{\mu\nu} = \bar{g}_{\mu\kappa} \left(e^{h \cdot} \right)_{\nu}^{\kappa}$

path integral:

$$\int \mathcal{D}g_{\mu\nu} e^{-S[g_{\mu\nu}]} \rightarrow \int \mathcal{D}h_{\mu\nu} e^{-S[\bar{g}_{\mu\nu} + h_{\mu\nu}]}$$

scale setting:

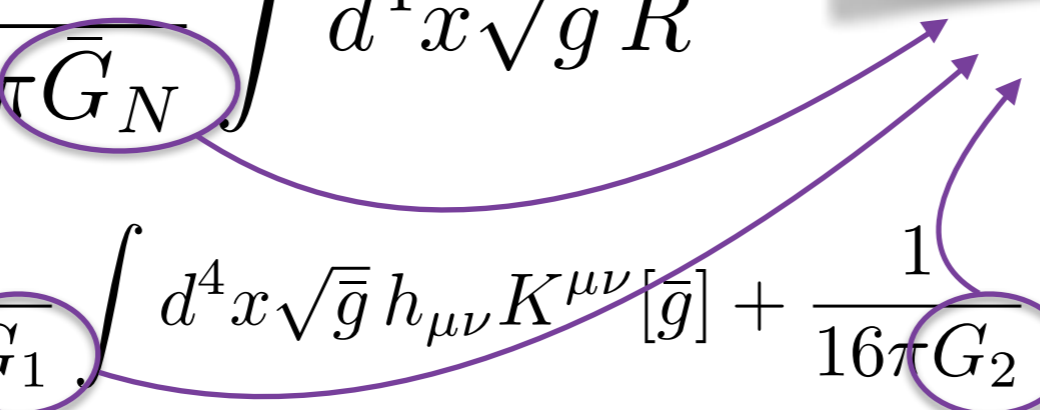
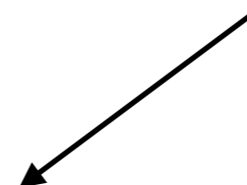
$$h_{\mu\nu} R_{\kappa}^{\mu\nu\kappa\lambda} (-\bar{D}^2) h_{\kappa\lambda}$$

$$S[g_{\mu\nu}] = -\frac{1}{16\pi G_N} \int d^4x \sqrt{g} R$$

$$= -\frac{1}{16\pi \bar{G}_N} \int d^4x \sqrt{\bar{g}} \bar{R}$$

$$-\frac{1}{16\pi G_1} \int d^4x \sqrt{\bar{g}} h_{\mu\nu} K^{\mu\nu}[\bar{g}] + \frac{1}{16\pi G_2} \int d^4x \sqrt{\bar{g}} h_{\mu\nu} h_{\kappa\lambda} K^{\mu\nu\kappa\lambda}[\bar{g}] + \dots$$

$$\beta_{\bar{G}_N} \neq \beta_{G_1} \neq \beta_{G_2} \dots$$



Matter matters

$$\beta_{\bar{G}} = 2\bar{G} - \frac{\bar{G}^2}{48\pi} (26(4 - \eta_h) + 20(4 - \eta_c) - N_S(4 - \eta_S) - N_D(4 - \eta_D) + 2N_V(8 - \eta_V))$$

Donà, A.E., Percacci '13, '14

destabilizing effect

one-loop result: Standard Model degrees of freedom compatible with grav. fixed point

Matter matters

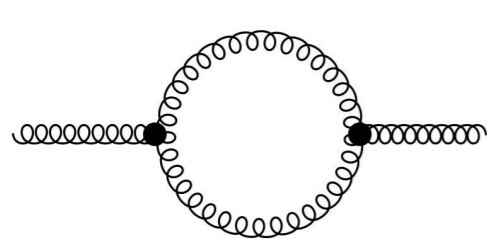
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Donà, A.E., Percacci '13, '14

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Where do fluctuation couplings enter?



$$\Rightarrow \eta_h = \eta_h(G_3, G_4)$$

→ talk by J. Pawłowski

Matter matters

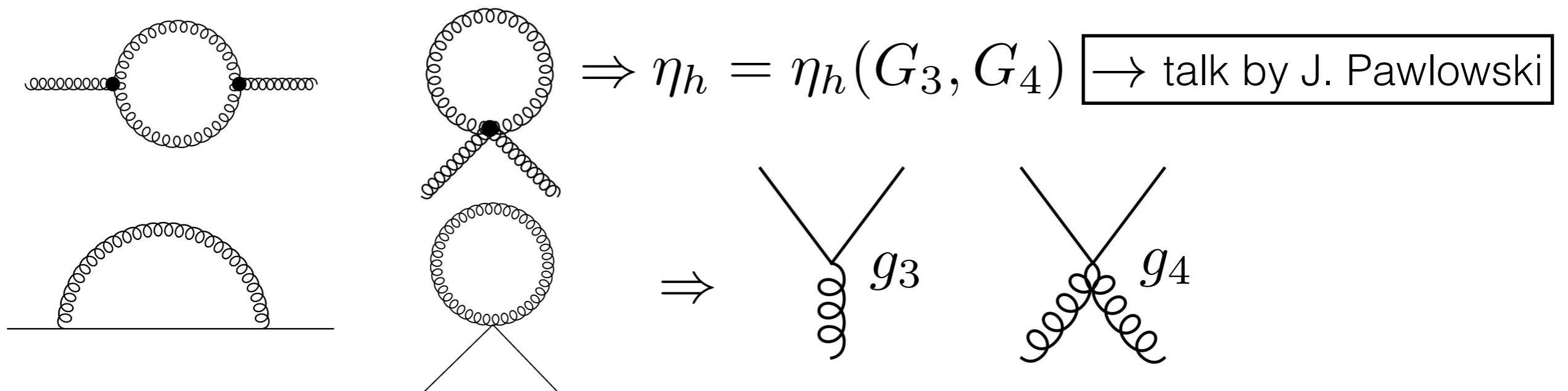
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Donà, A.E., Percacci '13, '14

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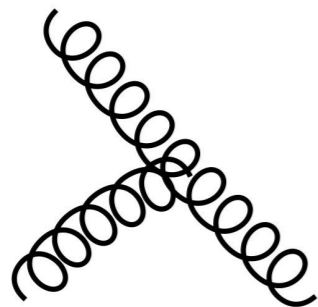


“Newton couplings” in gravity-matter systems

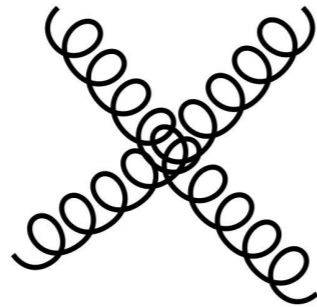
$$\hat{\Gamma} = -\frac{1}{16\pi G} \int d^4x \sqrt{g} R + S_{\text{gf}} + \frac{1}{2} \int d^4x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$$

$$g_{\mu\nu} = \bar{g}_{\mu\kappa} \left(e^{h \cdot} \right)_\nu^\kappa$$

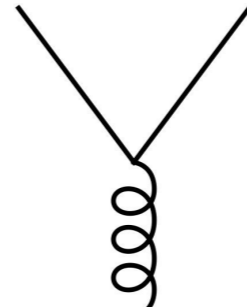
(unimodular gauge)



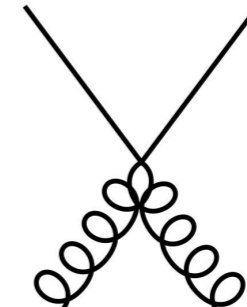
$\sqrt{G_3}$



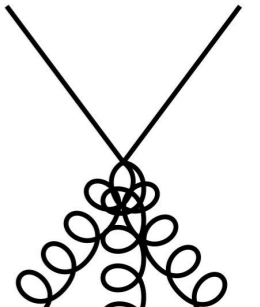
G_4



$\sqrt{g_3}$



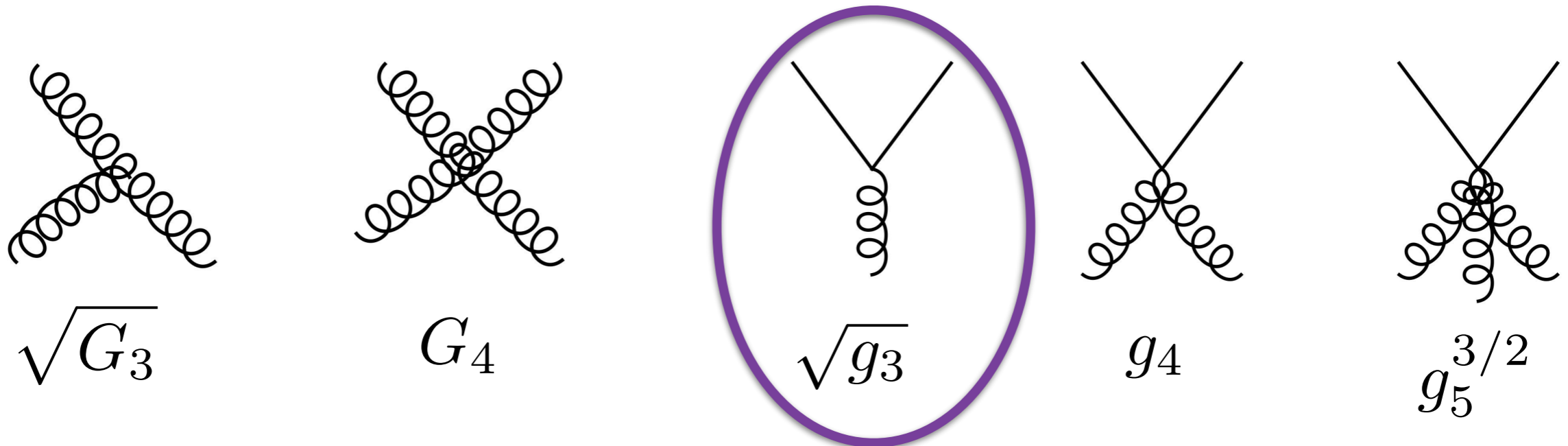
g_4



$g_5^{3/2}$

work in progress with P. Labus, P. Donà and R. Percacci

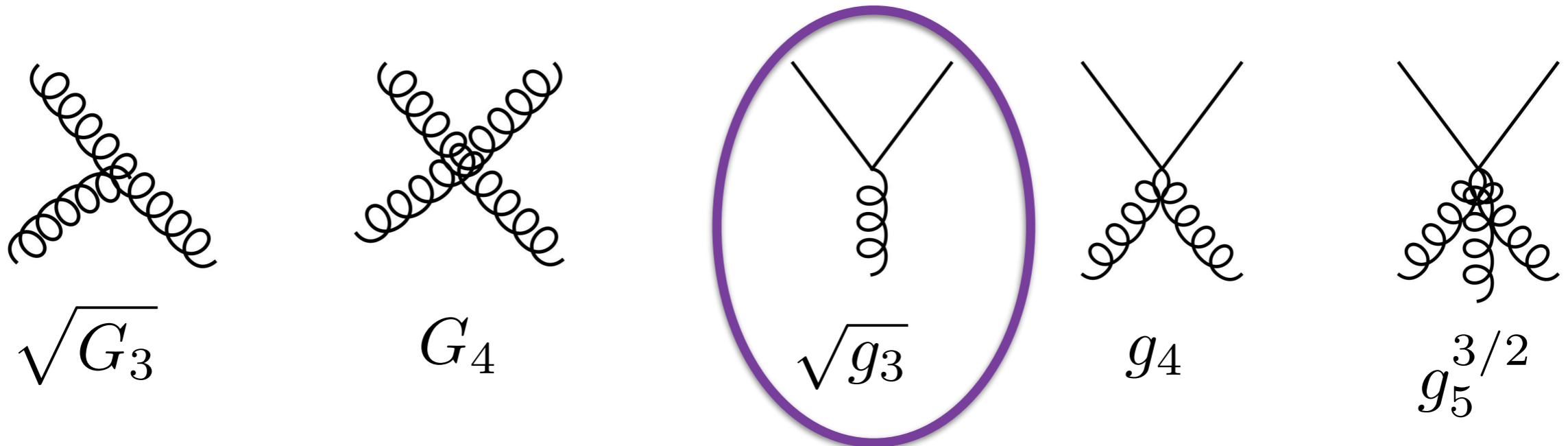
“Newton couplings” in gravity-matter systems



$$\begin{aligned}
 \beta_{g_3} = & (2 + \eta_{\text{TT}} + 2\eta_S) g_3 + \frac{3}{2\pi} g_3^2 + \frac{3}{2\pi} g_3^{3/2} \sqrt{G_3} - \frac{4}{\pi} g_3 g_4 - \frac{5}{18\pi} g_5^{3/2} \sqrt{g_3} \\
 & + \left(-\frac{5}{54\pi} g_4 \sqrt{G_3} + \frac{23}{108\pi} g_5^{3/2} \right) \sqrt{g_3} \eta_{\text{TT}} + \left(\frac{-1}{20\pi} g_3^{3/2} - \frac{1}{10\pi} g_3 \sqrt{G_3} + \frac{1}{4\pi} \sqrt{g_3} g_4 + \frac{5}{54\pi} g_4 \sqrt{G_3} - \frac{1}{6\pi} g_5^{3/2} \right) \sqrt{g_3} \eta_\sigma \\
 & + \left(-\frac{1}{10\pi} g_3^{3/2} - \frac{1}{20\pi} g_3 \sqrt{G_3} + \frac{1}{4\pi} \sqrt{g_3} g_4 \right) \sqrt{g_3} \eta_S
 \end{aligned}$$

work in progress with P. Labus, P. Donà and R. Percacci

“Newton couplings” in gravity-matter systems



$$\beta_{g_3} = (2 + \eta_{\text{TT}} + 2\eta_S) g_3 + \frac{3}{2\pi} g_3^2 + \frac{3}{2\pi} g_3^{3/2} \sqrt{G_3} - \frac{4}{\pi} g_3 g_4 - \frac{5}{18\pi} g_5^{3/2} \sqrt{g_3}$$

$$+ \left(-\frac{5}{54\pi} g_4 \sqrt{G_3} + \frac{23}{108\pi} g_5^{3/2} \right) \sqrt{g_3} \eta_{\text{TT}} + \left(\frac{-1}{20\pi} g_3^{3/2} - \frac{1}{10\pi} g_3 \sqrt{G_3} + \frac{1}{4\pi} \sqrt{g_3} g_4 + \frac{5}{54\pi} g_4 \sqrt{G_3} - \frac{1}{6\pi} g_5^{3/2} \right) \sqrt{g_3} \eta_\sigma$$

$$+ \left(-\frac{1}{10\pi} g_3^{3/2} - \frac{1}{20\pi} g_3 \sqrt{G_3} + \frac{1}{4\pi} \sqrt{g_3} g_4 \right) \sqrt{g_3} \eta_S$$

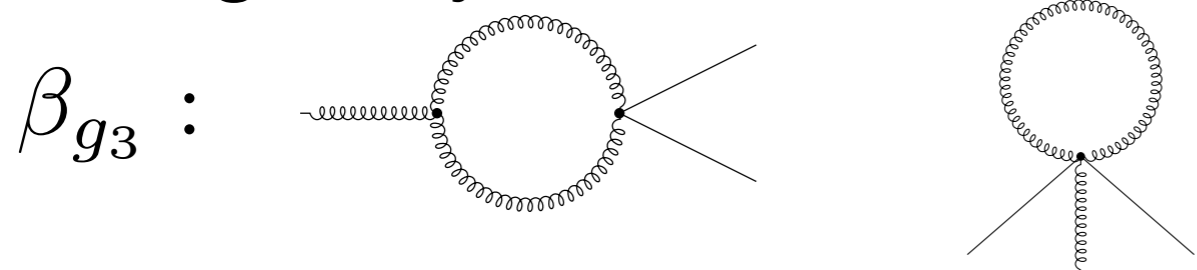
$$h_{\mu\nu} = h_{\mu\nu}^{TT} + \dots + \bar{D}^{-2} \bar{D}_\mu \bar{D}_\nu \sigma - \frac{1}{4} \bar{g}_{\mu\nu} \sigma$$

→ distinguish anomalous dimensions for graviton modes $\eta_{\text{TT}}, \eta_\sigma$

work in progress with P. Labus, P. Donà and R. Percacci

“Newton couplings” in gravity-matter systems

pure-gravity limit: no scalar fluctuations (only external lines)



$$g_5 = g_4 = G_3 = G_4 = g_3$$

$$g_{3*} = 4.58 \quad \theta = 2.27$$

$$\eta_{\text{TT}} = -1.24 \quad \eta_{\sigma} = 1.32$$

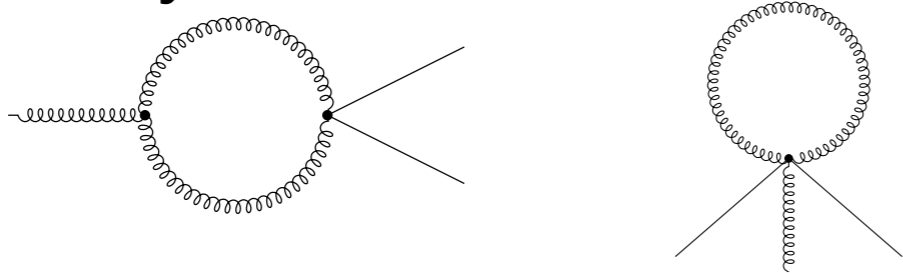
cf. background results:

$$\bar{G}_* = 3.68 \quad \theta = 2$$

[Vacca, Percacci, '15]

“Newton couplings” in gravity-matter systems

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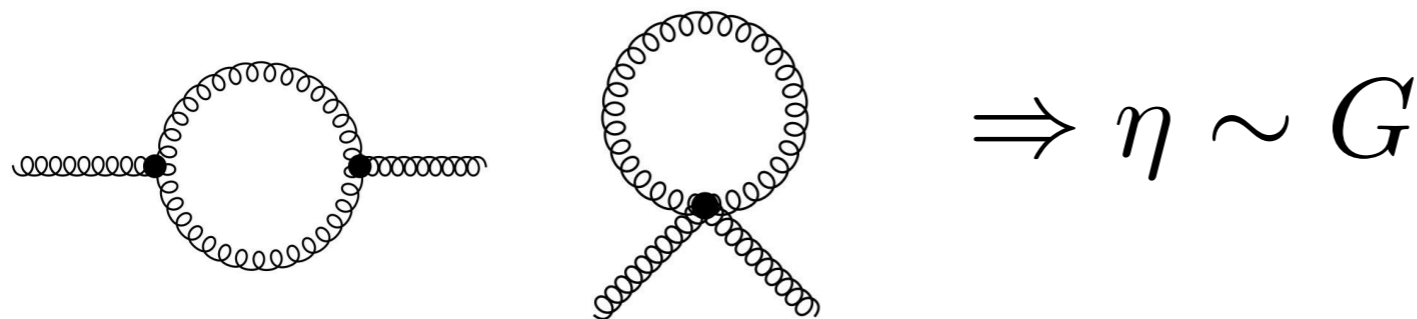


$$g_5 = g_4 = G_3 = G_4 = g_3$$

| | |
|---|---|
| $g_{3*} = 4.58$ $\eta_{\text{TT}} = -1.24$ | $\theta = 2.27$ $\eta_{\sigma} = 1.32$ |
|---|---|

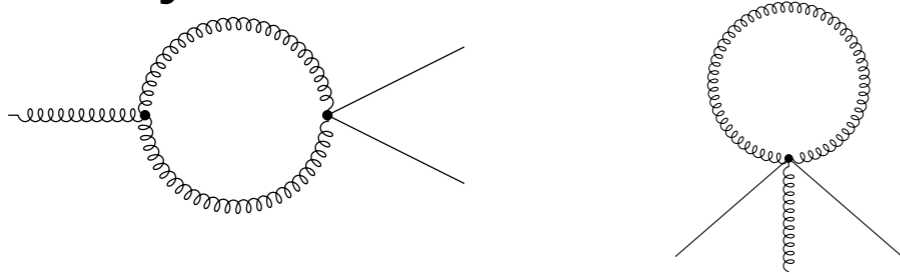
| | |
|---|--------------|
| cf. background results: $\bar{G}_* = 3.68$ [Vacca, Percacci, '15] | $\theta = 2$ |
|---|--------------|

cf. $\eta_h = 0.54$ (linear parameterisation) [Donà, Eichhorn, Percacci, '13]



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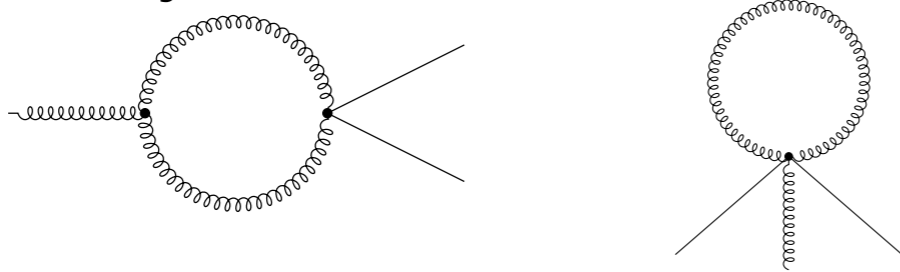
“dimensional reduction” of spacetime?

direction for the future:

distinguish tensor structures also in the vertices?

“Newton couplings” in gravity-matter systems

pure-gravity limit: no scalar fluctuations (only external lines)



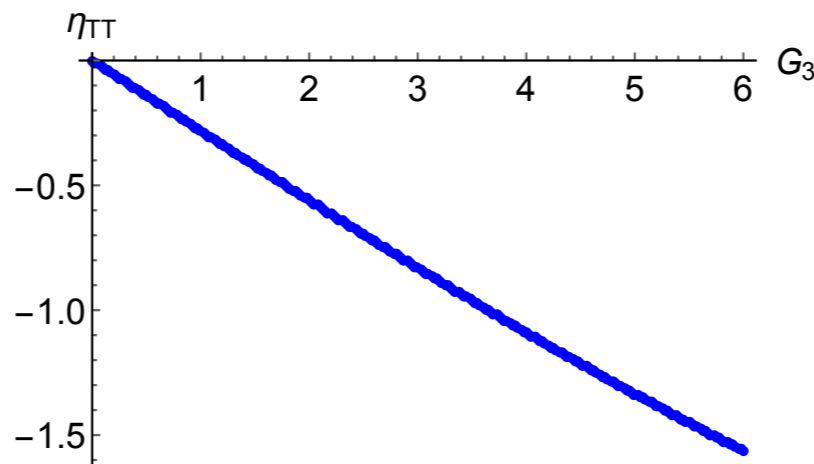
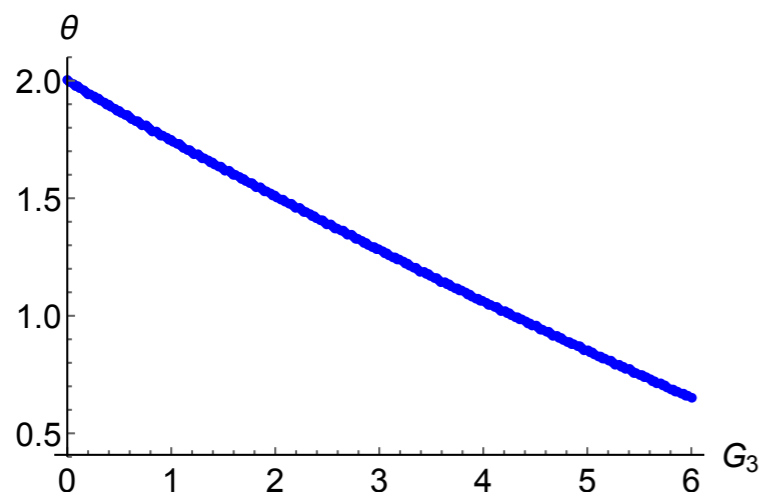
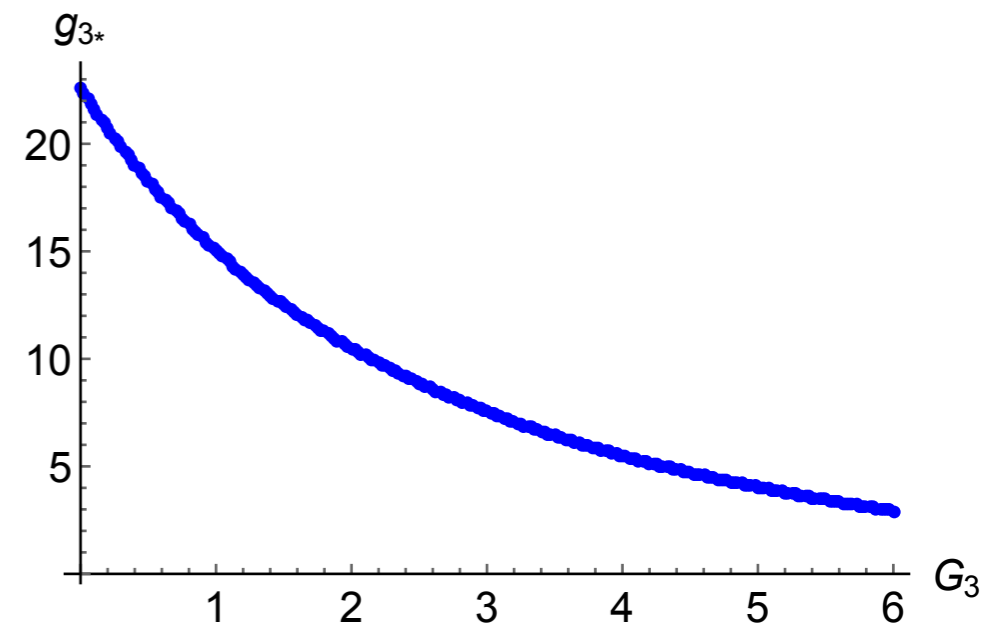
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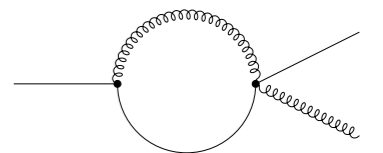
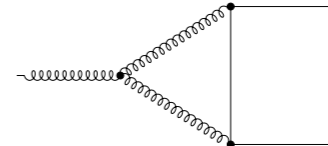
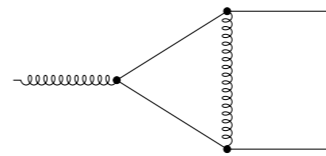
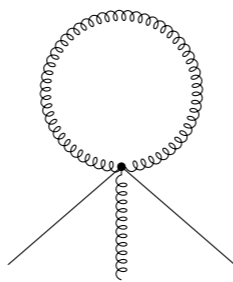
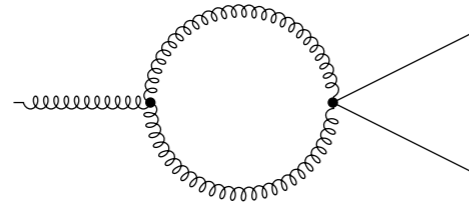


confirmation
of asymptotic
safety in fluctuation
couplings

“Newton couplings” in gravity-matter systems

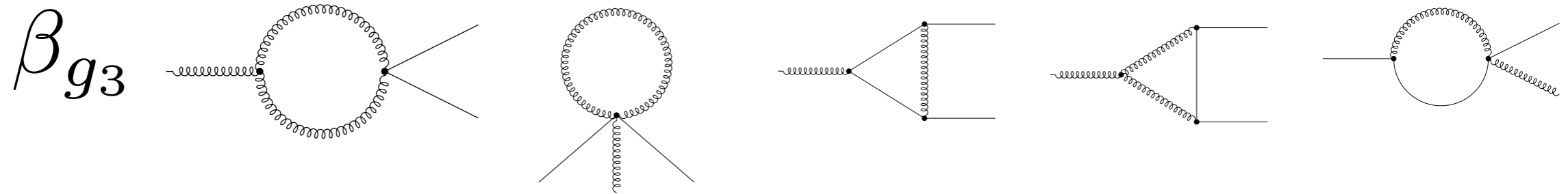
include scalar fluctuations (prelim. results)

β_{g_3}



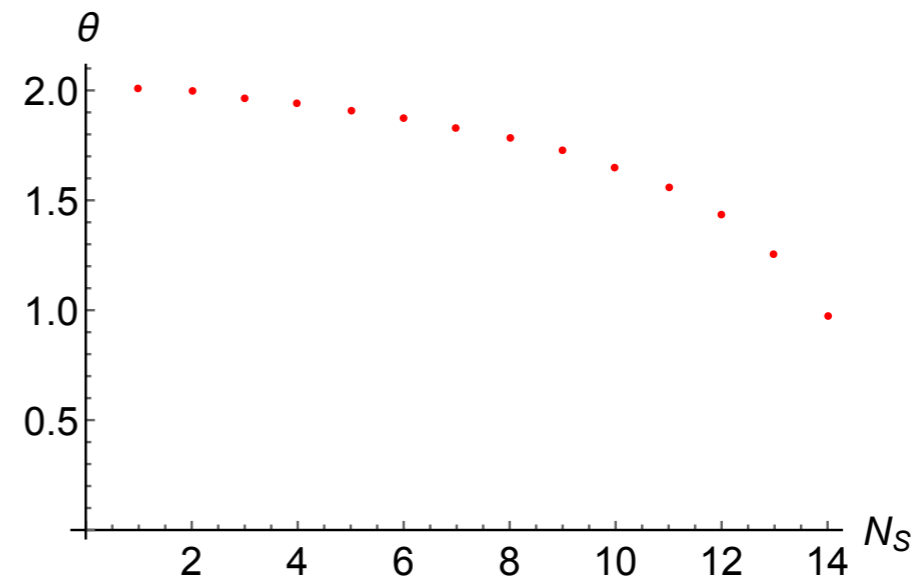
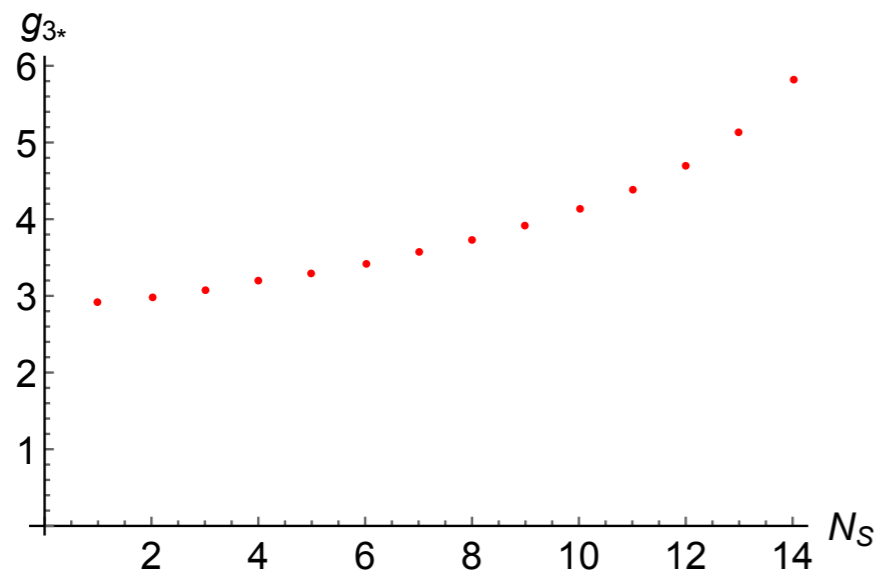
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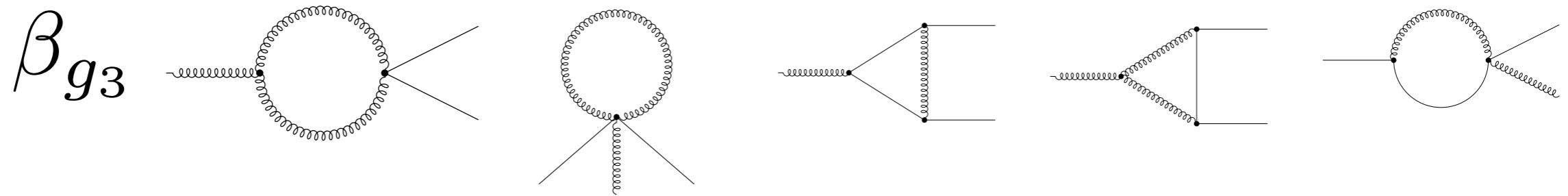
$$\eta_s = 0$$

$$\beta_{g_3} = 2g_3 - \frac{g_3^2}{6\pi} \left(13 - \frac{N_S}{4} \right) + \dots$$



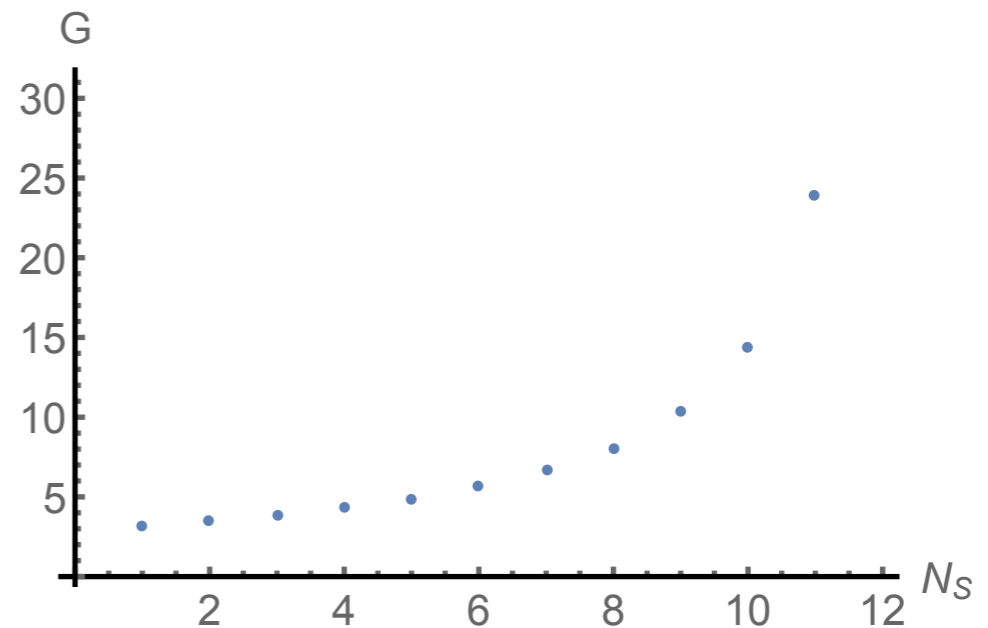
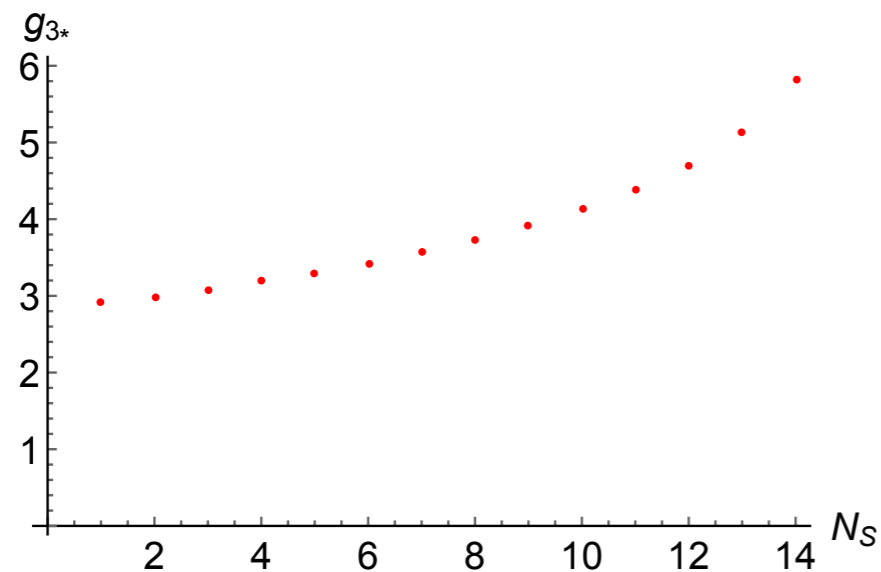
“Newton couplings” in gravity-matter systems

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$$\eta_s = 0$$

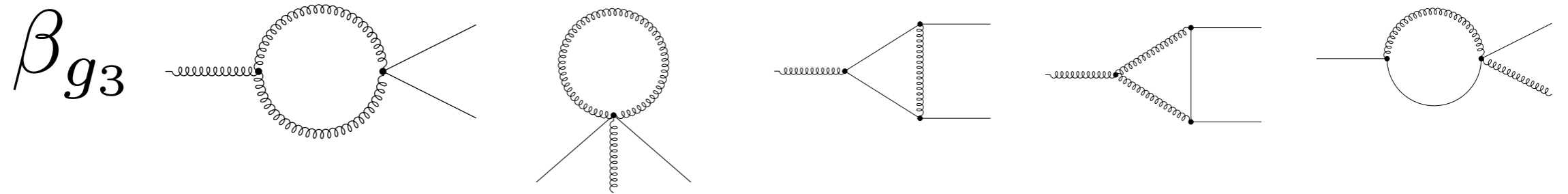
$$\beta_{g_3} = 2g_3 - \frac{g_3^2}{6\pi} \left(13 - \frac{N_S}{4} \right) + \dots$$



background coupling and fluctuation coupling similar

“Newton couplings” in gravity-matter systems

include scalar fluctuations (prelim. results)

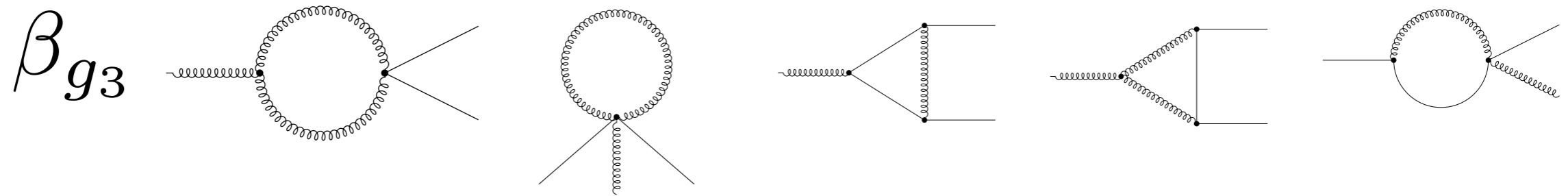


include η_s

$$\beta_{g_3} = 2g_3 - \frac{13}{6\pi}g_3^2 + \frac{g_3^2}{24\pi}N_S + 2g_3\eta_s + \dots \quad \eta_s = \frac{7}{4\pi}g_3$$

“Newton couplings” in gravity-matter systems

include scalar fluctuations (prelim. results)



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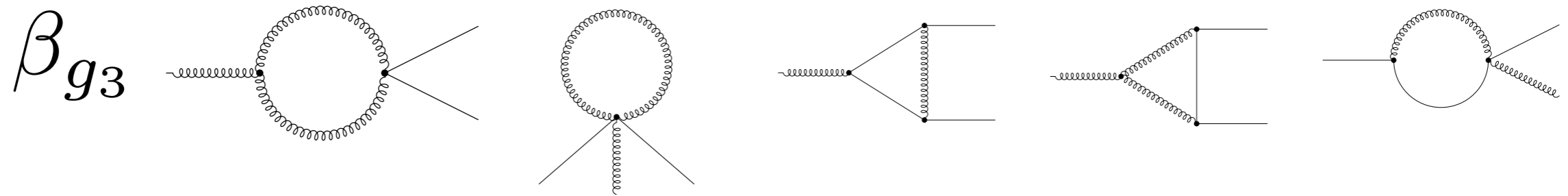
$$N_S = 1 : \quad g_{3*} = -7.2 \quad \theta = 1.18$$

$$g_i = G_i \quad \eta_{TT} = 1.88 \quad \eta_\sigma = -0.76 \quad \eta_s = -3.67$$

→ significant effects of scalar matter

“Newton couplings” in gravity-matter systems

include scalar fluctuations (prelim. results)



include η_s

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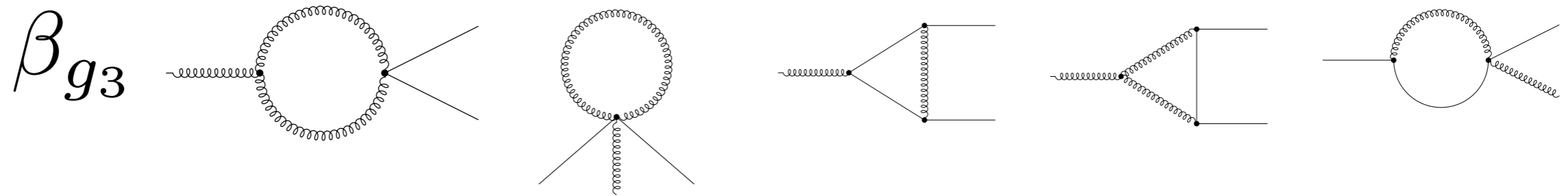
$$g_i = G_i \quad \eta_{TT} = 1.88 \quad \eta_\sigma = -0.76 \quad \eta_s = -3.67$$

→ significant effects of scalar matter

$N_S = 1.8$: fixed-point annihilation

“Newton couplings” in gravity-matter systems

include scalar fluctuations (prelim. results)



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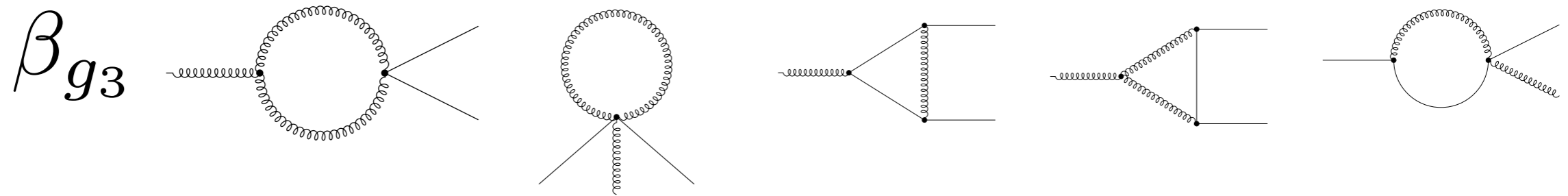
Future direction: Better truncation for η_s

$$\longrightarrow (\partial_{\mu}\phi\partial^{\mu}\phi)^2 \longrightarrow \eta_s$$

Gravity-induced matter self-interactions could play a role

“Newton couplings” in gravity-matter systems

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Future direction: Better truncation for η_s

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Gravity-induced matter self-interactions could play a role

Is there a difference between exponential and linear parameterization?

Summary

- asymptotic safety: joint model of gravity and matter

Summary

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- fixed point is fully non-Gaussian

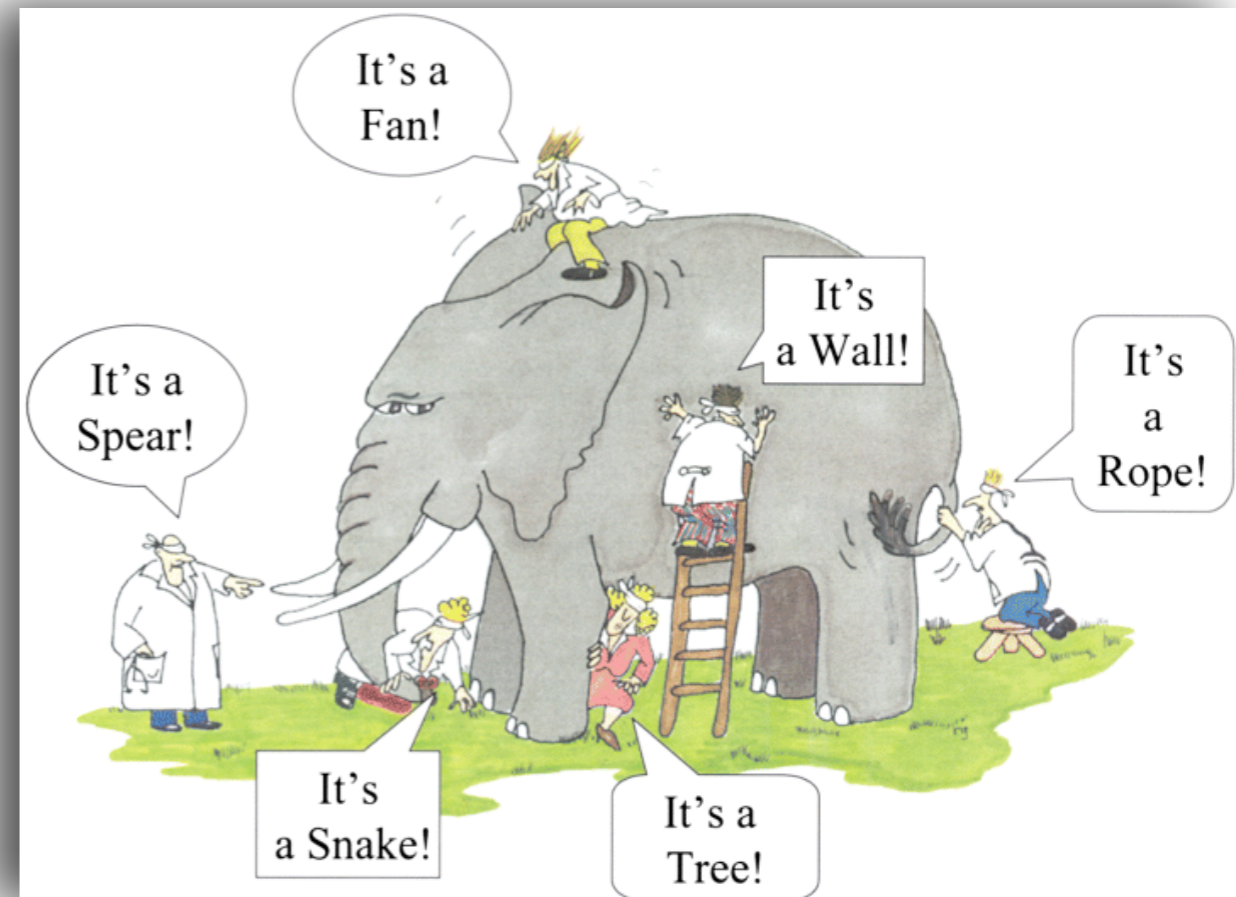
Summary

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What is the gravity-matter dynamics in the UV?



Summary

- asymptotic safety: joint model of gravity and matter
- fixed point is fully non-Gaussian
- Newton coupling defined from gravity-matter vertex exhibits asymptotic safety in pure-gravity case and in certain approximation also for small number of scalars

Future directions

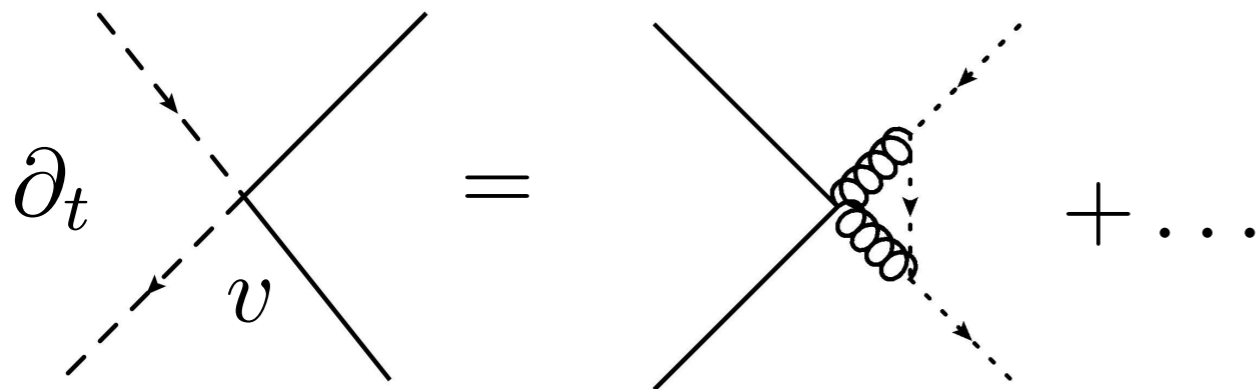
- Explore matter-gravity vertices in larger truncations, linear parameterisation
- Which marginal SM couplings are irrelevant at an interacting fixed point?
- What about asymptotic freedom in gauge theories coupled to asymptotically safe gravity?

Structure of a fixed point for gravity + matter

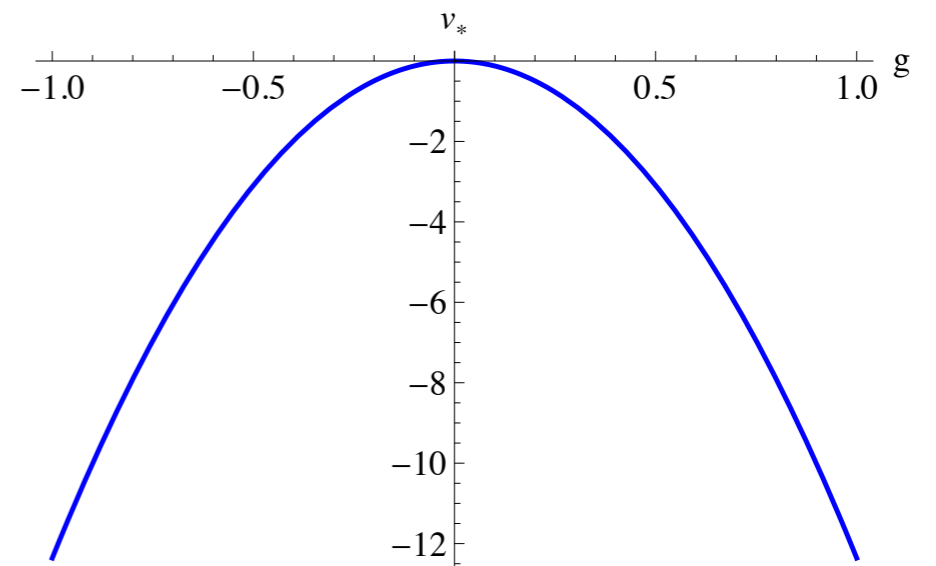
$$\int d^d x \sqrt{g} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$$

$$\Gamma_{\text{Faddeev-Popov}}$$

$$= -\sqrt{2} \int \bar{c}_\mu \left(\bar{D}^\rho \bar{g}^{\mu\kappa} g_{\kappa\nu} D_\rho + \dots \right) c^\nu$$



A.E., '13



no “simple” FP ghost sector at fixed point