

Gravitational-Wave Observations of Compact Binary Mergers

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PHAROS

THE MULTI-MESSENGER
PHYSICS AND ASTROPHYSICS
OF NEUTRON STARS

PhD School Jena



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- Today's technology
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- Status

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4 GW150914

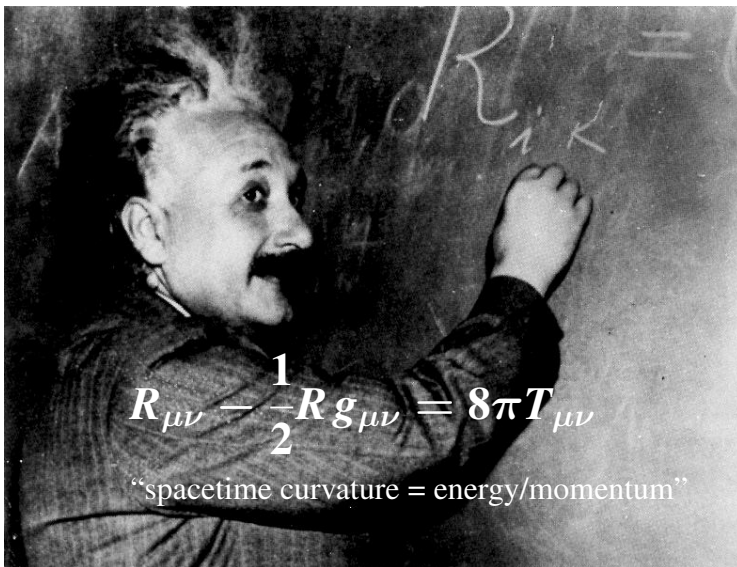
- Discovery
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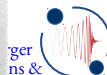
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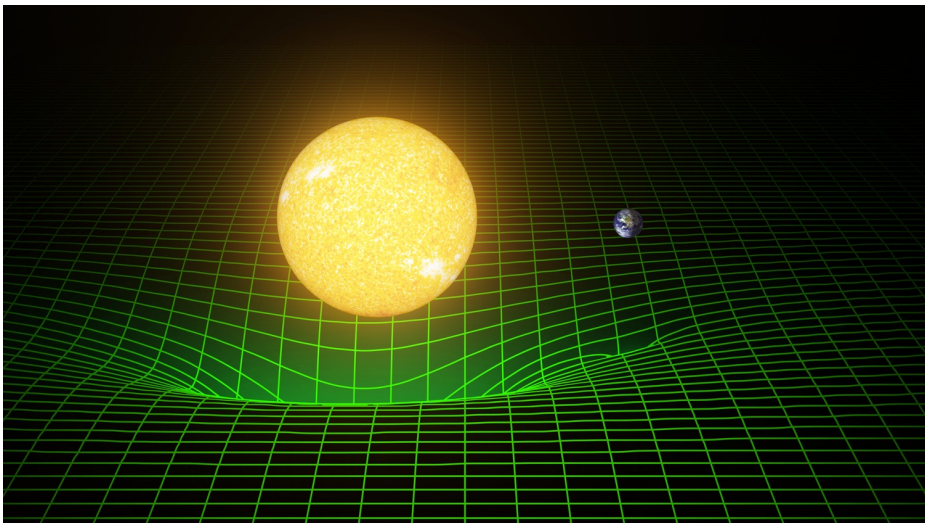
- GWTC-1
- GW170817
- Getting involved



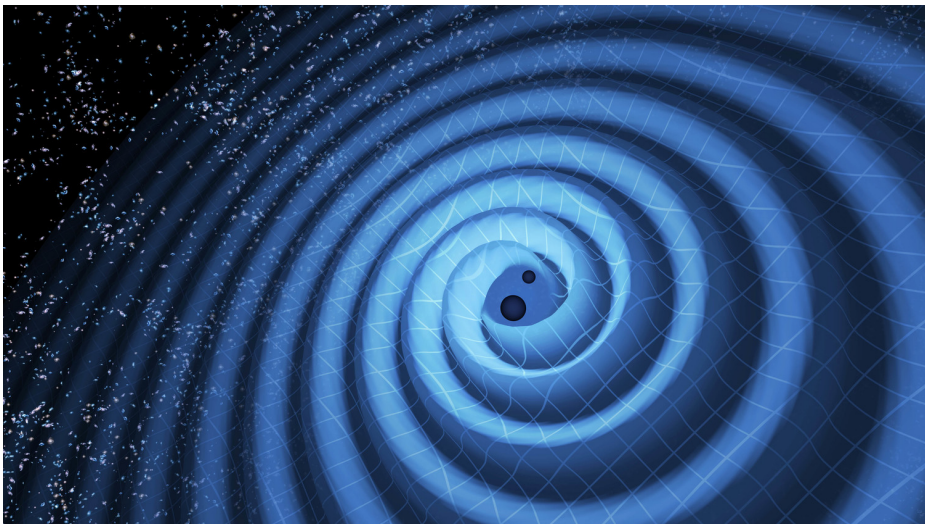
$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi T_{\mu\nu}$$

“spacetime curvature = energy/momentum”





Credit: T. Pyle/Caltech/MIT/LIGO Lab



Credit: LIGO/T. Pyle



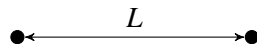
Linearised theory

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}, \quad |h_{\mu\nu}| \ll 1$$

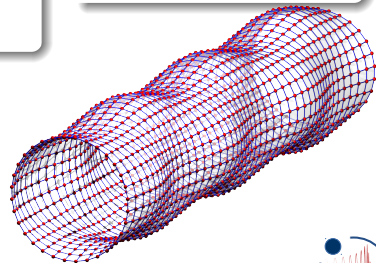
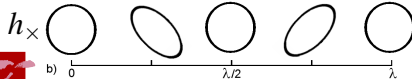
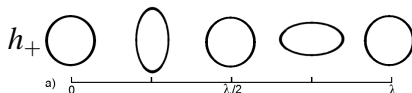
$$\Rightarrow \text{(Lorentz gauge)} \quad \square \bar{h}_{\mu\nu} = -16\pi T_{\mu\nu}$$

$$h_{\mu\nu} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & h_+ & h_\times & 0 \\ 0 & h_\times & -h_+ & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \Rightarrow \text{Gravitational waves}$$

Effect



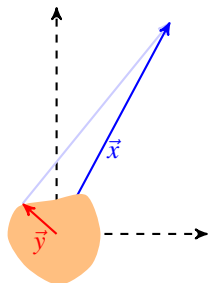
$$\frac{\delta L}{L} \approx \frac{h_+}{2}$$



Solution of the wave equation

$$\begin{aligned}\bar{h}_{ij}(t, \vec{x}) &= 4 \int \frac{T_{ij}(t - |\vec{x} - \vec{y}|, \vec{y})}{|\vec{x} - \vec{y}|} d^3y \\ &\approx \frac{2}{|\vec{x}|} \frac{d^2}{dt^2} \int y^i y^j \rho(t - |\vec{x}|, \vec{y}) d^3y\end{aligned}$$

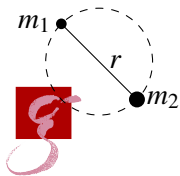
(for $|\vec{x}| \gg |\vec{y}|$, finite-size, non-relativistic sources)



Newtonian binary

Assume the perfect circular motion of two point particles $m_1 = m_2$ with a constant orbital frequency ω .

- 1 Parameterize the position of both particles $\vec{x}_1(t)$, $\vec{x}_2(t)$.
- 2 Use $\rho(t, \vec{y}) = m_1 \delta(\vec{y} - \vec{x}_1) + m_2 \delta(\vec{y} - \vec{x}_2)$ to calculate \bar{h}_{ij} .



Solution

Centre-of-mass coordinate system:

$$\vec{x}_1 = \left[\frac{r}{2} \cos(\omega t), \frac{r}{2} \sin(\omega t) \right] = -\vec{x}_2$$

$$\int y^1 y^1 \rho(t, \vec{y}) d^3 y = m_1 \frac{r^2}{4} \cos^2(\omega t) + m_2 \frac{r^2}{4} \cos^2(\omega t) = \frac{Mr^2}{4} \cos^2(\omega t)$$

$$\int y^i y^j \rho(t, \vec{y}) d^3 y = \frac{Mr^2}{4} \begin{pmatrix} \cos^2(\omega t) & \cos(\omega t) \sin(\omega t) \\ \cos(\omega t) \sin(\omega t) & \sin^2(\omega t) \end{pmatrix}$$

$$= \frac{Mr^2}{8} \begin{pmatrix} 1 + \cos(2\omega t) & \sin(2\omega t) \\ \sin(2\omega t) & 1 - \cos(2\omega t) \end{pmatrix}$$

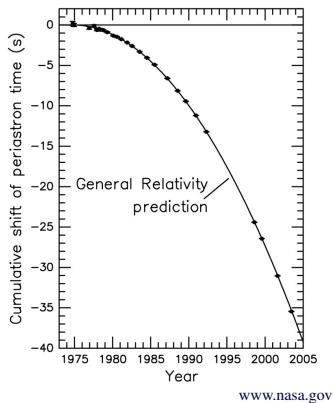
$$\bar{h}_{ij}(t, \vec{x}) = -\frac{Mr^2 \omega^2}{|\vec{x}|} \begin{pmatrix} \cos(2\omega t') & \sin(2\omega t') \\ \sin(2\omega t') & -\cos(2\omega t') \end{pmatrix}$$

$$t' = t - |\vec{x}|$$



Observational evidence

Hulse-Taylor pulsar 1978,
Nobel prize 1993



Some numbers

- $m_1 = 1.441M_\odot$

- $m_2 = 1.387M_\odot$

⇒ $M = 2.828M_\odot$

- $D \approx 6.4 \text{ Mpc}$

- $P \approx 7.75 \text{ hr}$

⇒ $\omega_{\text{orb}} \approx 2.25 \times 10^{-4} \text{ s}^{-1}$

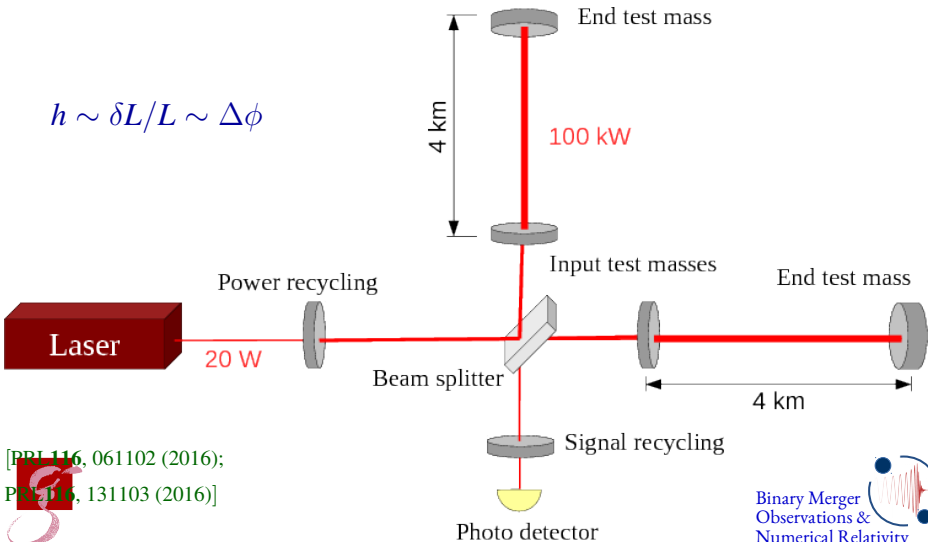
- $r \sim 10^6 \text{ km}$

⇒ $h \sim \mathcal{O}(10^{-26})$

[for comparison (in metres): Carbon atom radius $\mathcal{O}(10^{-10})$, proton radius $\mathcal{O}(10^{-15})$, earth-moon $\mathcal{O}(10^8)$, earth-sun $\mathcal{O}(10^{11})$]

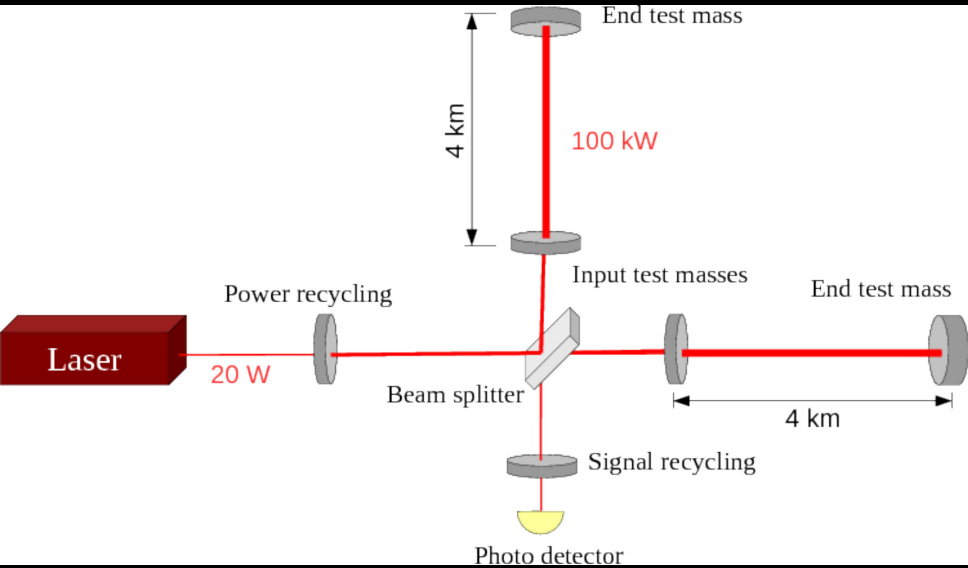
Catching Gravitational Waves

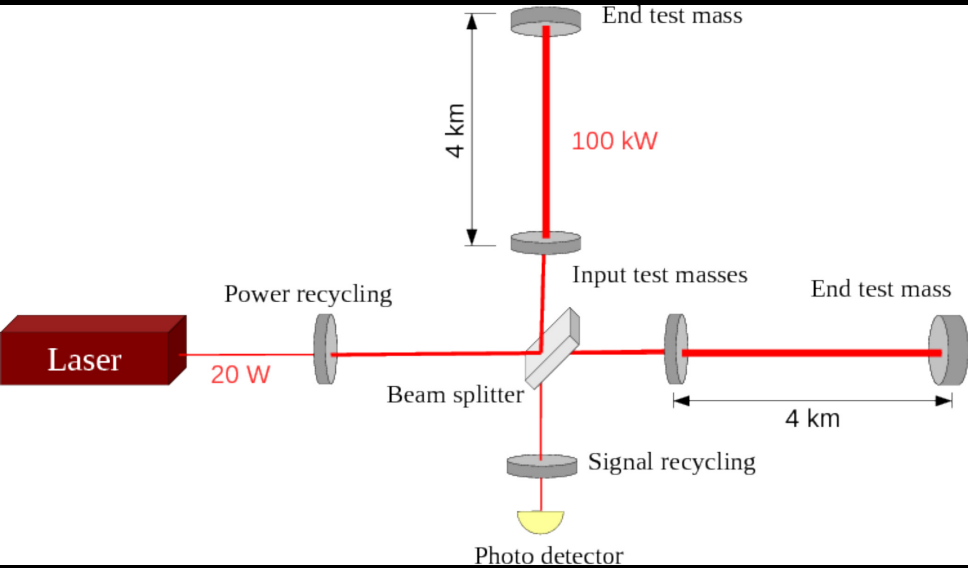
$$h \sim \delta L/L \sim \Delta\phi$$



[PRL 116, 061102 (2016);

PRL 116, 131103 (2016)]





Today's technology

LIGO Hanford



Binary Merger
Observations &
Numerical Relativity



Today's technology

LIGO Livingston



Binary Merger
Observations &
Numerical Relativity



Today's technology

Inside LIGO: The tube



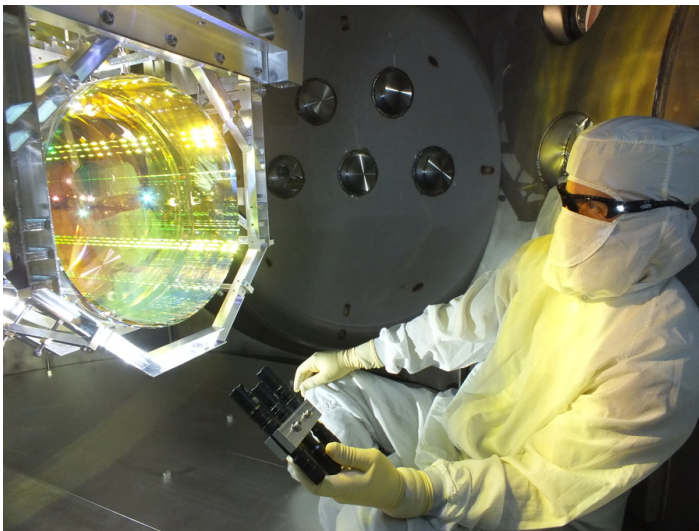
Today's technology

Inside LIGO: Laser and vacuum equipment



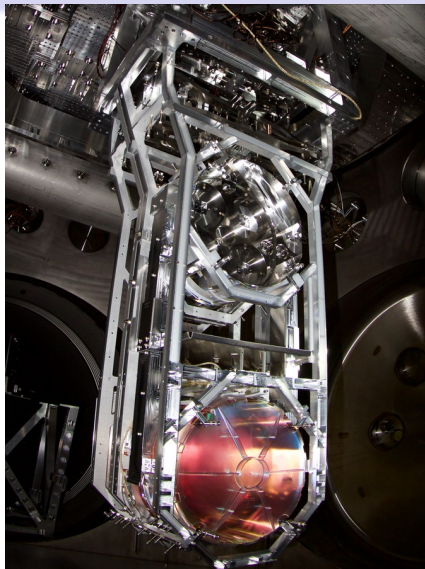
Today's technology

Inside LIGO: Optics



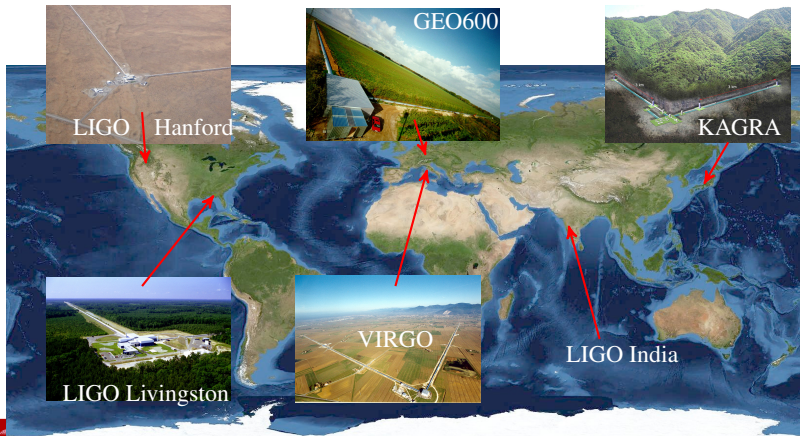
Today's technology

Inside LIGO: Suspension



Detector network

The GW detector network

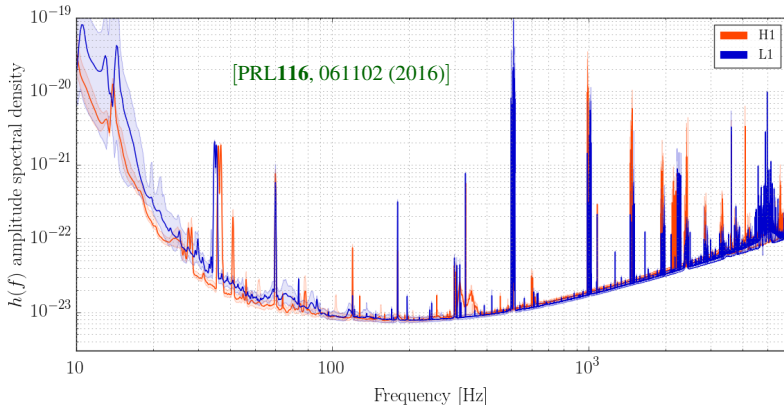


Status

Instrument noise

Seismic Ground vibrations
 Thermal Finite temperature
 Quantum Light quanta

Gravity gradient Gravitational field
 of the environment



aLIGO LHO Logbook

Logbooks LHO LLO Virgo KAGRA

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Reports until 15:06, Tuesday 05 March 2019

H1 PSL

jason.oberling@LIGO.ORG - posted 15:06, Tuesday 05 March 2019 (47307)

PSL Work Today

P. King, R. Savage, J. Oberling, D. Sigg

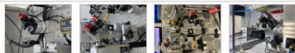
FSS RefCav Picomotor Mirror Mounts

At the request of the LHO commissioning team, today we installed 2 picomotor equipped mounts in the FSS RefCav path. We replaced the mount for mirror M2 the FSS EOM, 1st attachment) and for the upper periscope mirror (UPM, 2nd attachment). We used M27 instead of the lower periscope mirror (LPM) because it is to the RefCav; with this setup, M27 primarily changes beam position while the UPM primarily changes beam angle. The 3rd attachment shows both new picomotor

The same driver (PICO D) that runs the picomotors for the PMC input mirrors (mirrors M06 and M07) had 2 empty channels, so we used these for the new RefCav of now, channels 1 & 2 are for the PMC picomotor mirrors and channels 3 & 4 are for the RefCav; Daniel changed the displayed channel names on the picomotor screen to reflect this. To end, we confirmed that all picomotors functioned as expected, which they did. When we left the enclosure the FSS RefCav TPD read - was transmitting **-54.5W**. During the next maintenance window where we **do not** have an enclosure incursion, I will tweak the alignment into both the PMC and

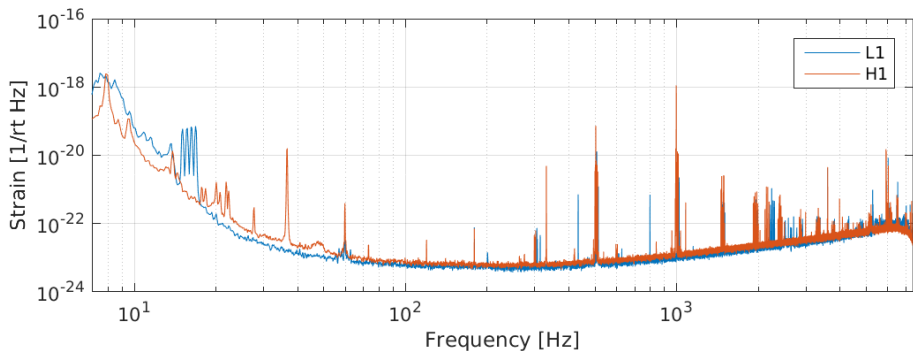
70W Amplifier Power Monitor PD

We had noticed some odd behavior with the 70W amp power monitor PD (the PD that the 70W amp power watchdog triggers off of). When blocked directly at the PSL Beckhoff software reports $\sim 3W$ on this PD; when blocked farther away the reading is $\sim 52W$. We suspected the cause to be room lights, so we added a tube (808nm pump light filter) screwed onto the end (4th attachment); this second RG850 was added to block more of the room light, as one wasn't quite enough. The blocked reading to $\sim 3W$ regardless of how far away the blockage occurred, with no degradation in the amount of power read by the PD when unblocked.

Images attached to this report**H1 CDS (CDS, DCS)**

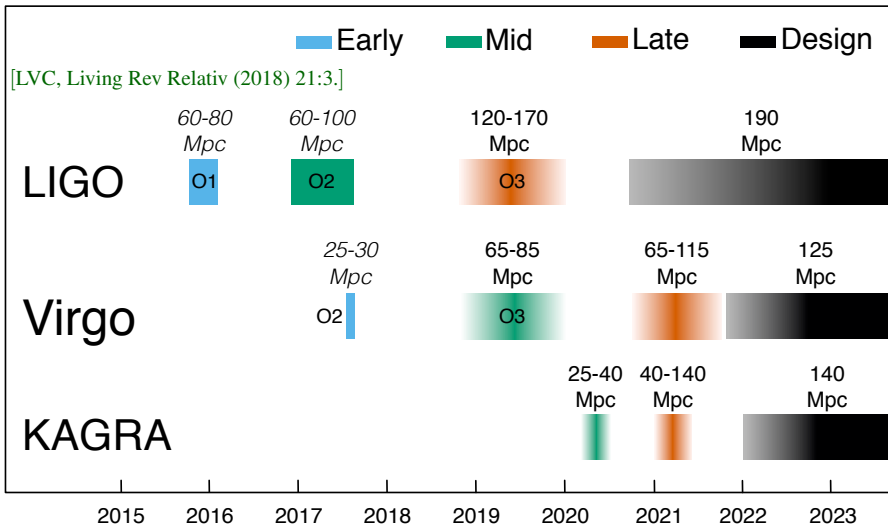
gregory.mendell@LIGO.ORG - posted 13:05, Tuesday 05 March 2019 - last comment - 13:28, Tuesday 05 March 2019(47302)

DMT computers have been patched and rebooted, bringing in gds2.18.16-1.e17
<https://alog.ligo-wa.caltech.edu/aLOG>

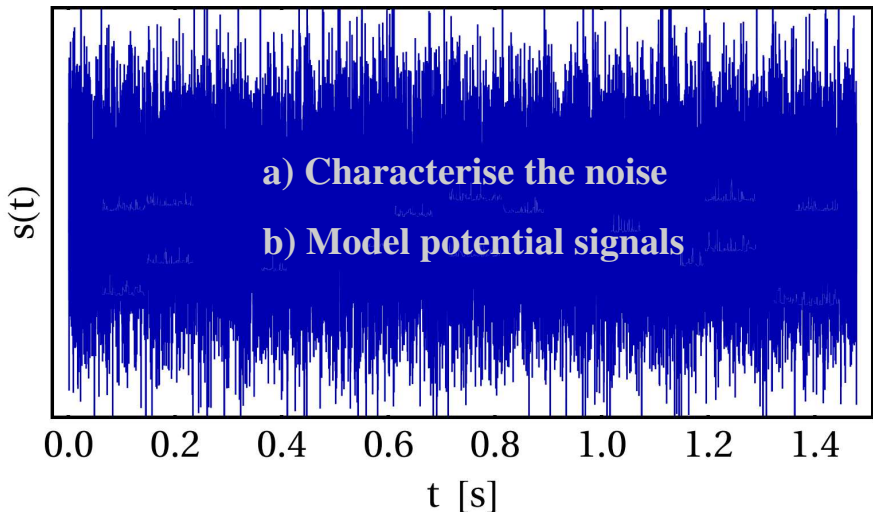



(post by Sheila Dwyer, 01 March 2019)
 average binary-neutron-star range $\gtrsim 100$ Mpc





Typical data stream



Theory of Stationary Gaussian noise

- **Assume** the following noise properties:
 - Stationarity: invariant under time translation
 - Gaussianity with zero mean
- Fourier spectrum of the noise:

$$\tilde{n}_T(f) = \frac{1}{\sqrt{T}} \int_0^T n(t) e^{-i2\pi f t} dt$$

$$S_n(f) = \left\langle \lim_{T \rightarrow \infty} |\tilde{n}_T(f)|^2 \right\rangle$$

- Wiener-Khinchin theorem: S_n is the Fourier transform of the auto-correlation function

$$\Rightarrow \langle \tilde{n}(f) \tilde{n}^*(f') \rangle = \frac{1}{2} S_n(f) \delta(f - f')$$



Signal buried in the noise?

- How **likely** is a particular noise realisation?

$$p(n) \sim e^{-(n|n)/2},$$

with $(a|b) = 4 \operatorname{Re} \int \frac{\tilde{a}(f) \tilde{b}^*(f)}{S_n(f)} df$.

- Is it likely that the observed data stream s contains a signal h , i.e., $s = n + h$?

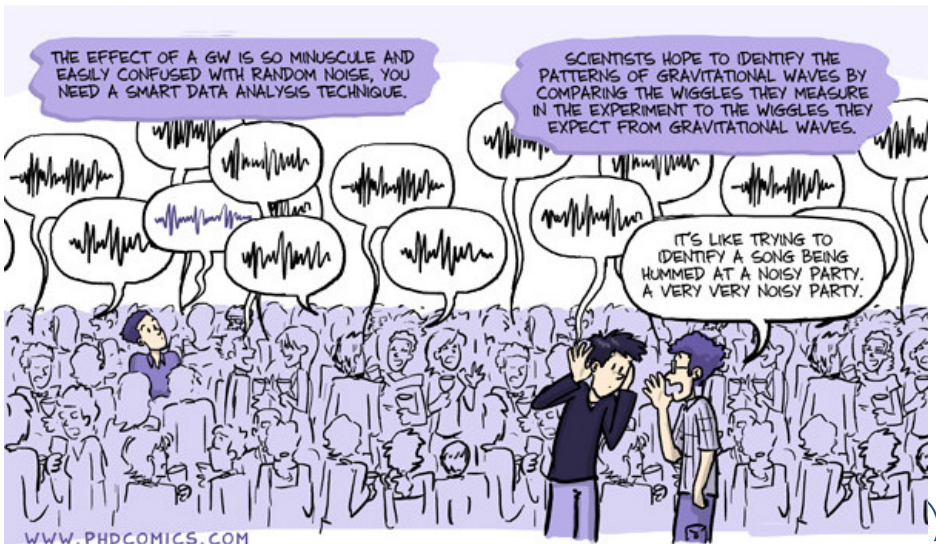
$$\Lambda = \frac{e^{-(s-h|s-h)/2}}{e^{-(s|s)/2}}$$

$$\ln \Lambda = (s|h) - \frac{(h|h)}{2} \leq \frac{1}{2} \frac{(s|h)}{\sqrt{(h|h)}} = \frac{1}{2} (s|\hat{h})$$

$(s|\hat{h})$ is commonly referred to as the (recovered) signal-to-noise ratio

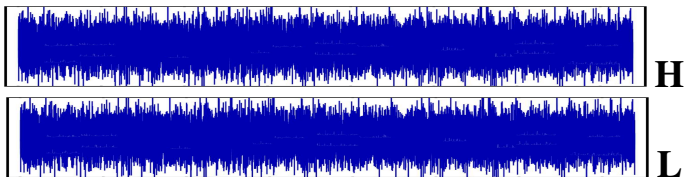


Matched filtering



Real-life Searches

- ① Need to know the signals we are looking for.
- ② Filter data with all some of them.
- ③ Account for non-stationarity and non-Gaussianity of noise.
- ④ Quantify false alarm probability.



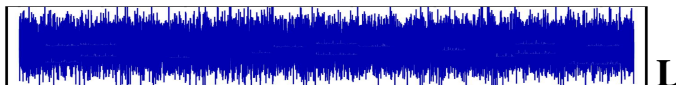
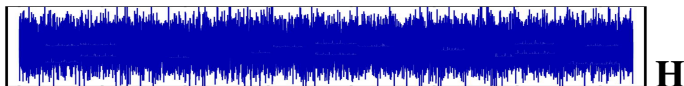
coherent signal?



Matched filtering

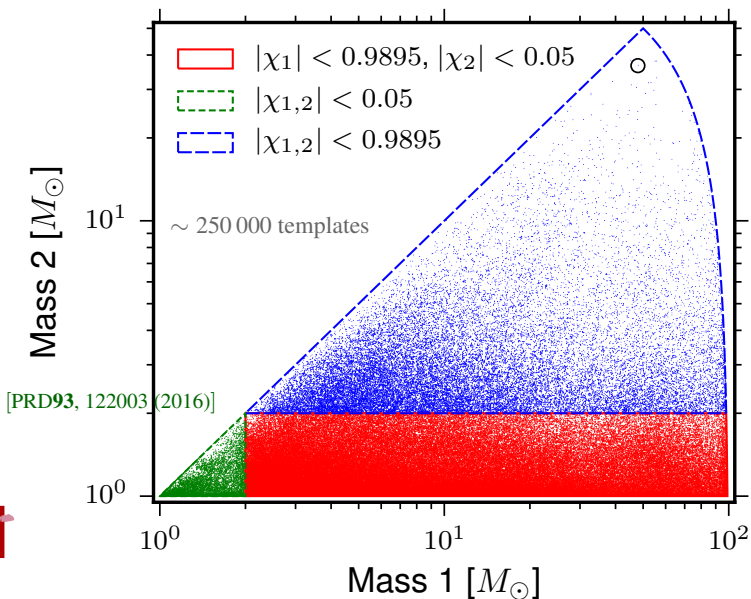
Real-life Searches

- ① Need to know the signals we are looking for.
- ② Filter data with all some of them.
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- ④ Quantify false alarm probability.

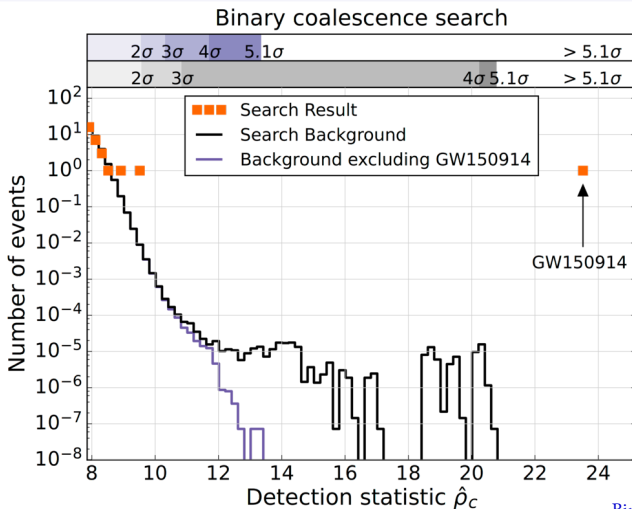


No coherent signal!

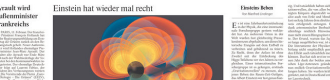


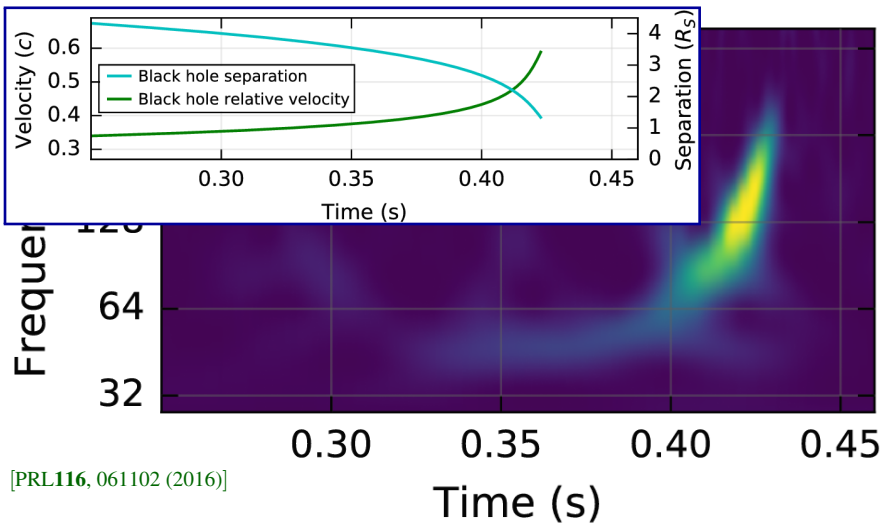


Matched filtering

Search results – PRL**116**, 061102 (2016) & PRD**93**, 122003 (2016)







[PRL116, 061102 (2016)]





Universitat
de les Illes Balears

Binary phase evolution

Newtonian binary (arbitrary masses)

$$\begin{aligned} h(t) &= F_+ h_+ + F_\times h_\times \\ &= \mathcal{A} \frac{4M\eta v(t)^2}{D} \cos(2\phi_{\text{orb}}(t) + \phi_0) \end{aligned}$$

$$E(t) = -\frac{M\eta}{2} v(t)^2$$

$$\mathcal{L}(t) = \frac{32}{5} \eta^2 v^{10}(t)$$

$$v(t) = \omega(t) r(t)$$

$$\eta = \frac{m_1 m_2}{M^2}$$

Kepler's law:

$$v^2(t) = \frac{M}{r(t)}$$

Newtonian phase evolution

- From the energy-balance law, $dE/dt = -\mathcal{L}$, derive a differential equation for the binary's velocity $v(t)$.
- Calculate $v(t)$ and $\omega(t)$.
- Integrate $\omega(t)$ to obtain $\phi_{\text{orb}}(t)$.

Solution

$$\frac{dv}{dt}(t) = -\frac{\mathcal{L}(t)}{dE(v)/dv} = \frac{32}{5M}\eta v^9(t)$$

$$v(t) = \frac{1}{2} \sqrt[8]{\frac{5M}{\eta(t_c - t)}}$$

$$\omega(t) = \frac{v^3(t)}{M} = \frac{1}{8} \left(\frac{5}{M^{5/3} \eta(t_c - t)} \right)^{3/8} = \frac{1}{8M_c^{5/8}} \left(\frac{5}{t_c - t} \right)^{3/8}$$

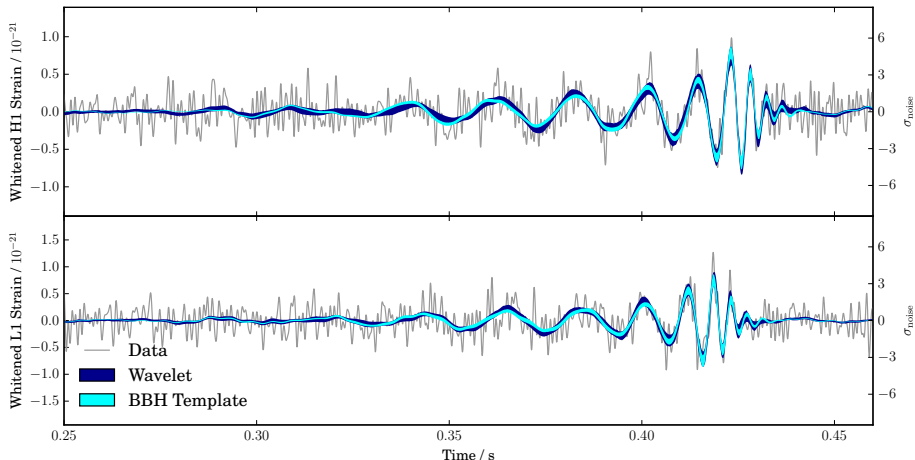
$$M_c = M \eta^{3/5}$$

$$\phi_{\text{orb}}(t) = \int \omega(t) dt = \phi_c - \left(\frac{t_c - t}{5M_c} \right)^{5/8}$$



Inspiral evolution

GW150914



[PRL116, 241102 (2016)]

How much mass is in the system?

see also [LVC 1608.01940]

Binary Merger
Observations &
Numerical Relativity

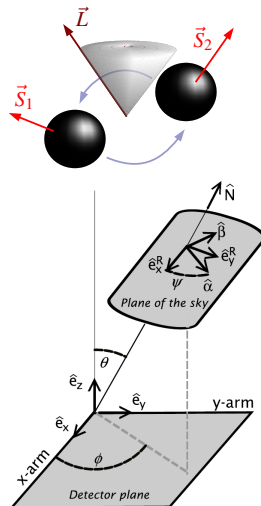
Binary parameters

Intrinsic parameters

- 2 masses ($m_1, m_2 / M_c, q$)
- 6 spin vector parameters
- reference time and phase
- ~~2 eccentricity parameters~~
- tidal parameters (for neutron stars)

Extrinsic parameters

- 2 angles for sky location
- inclination angle (ι)
- polarization angle (ψ)
- distance (D)



[Sathyaprakash, Schutz, LRR]

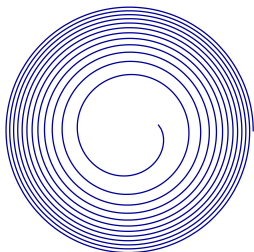
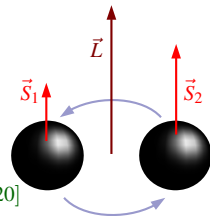
Spins

Non-precessing systems

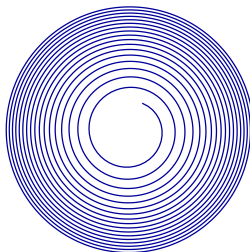
Aligned spins

- Parameters: M , η , $\chi_i = \frac{\vec{S}_i \cdot \hat{L}}{m_i^2}$
- Reduced spin: $\chi_{\text{eff}} = \frac{m_1 \chi_1 + m_2 \chi_2}{M}$

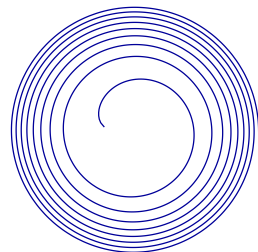
[Poisson, Will, 9502040; Ajith, 1107.1267, Pürrer *et al.*, 1306.2320]



$$q = 1, \chi_1 = \chi_2 = 0$$



$$q = 1, \chi_1 = \chi_2 = 0.99$$

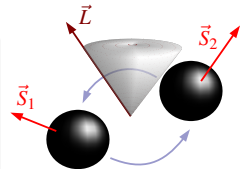


$$q = 1, \chi_1 = \chi_2 = -0.99$$

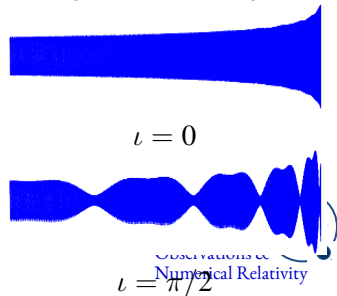
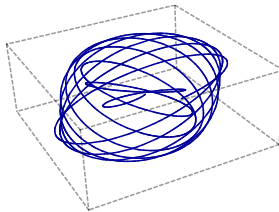
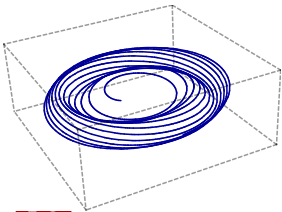
Generic spins: precession

Parameters

- $\eta, \vec{S}_1^\perp, \vec{S}_2^\perp \mapsto \eta, \chi_p$ [Schmidt, FO, Hannam 1408.1810]
- Waveform depends non-trivially on orientation, in particular inclination ι



[Hannam, 1312.3641]



Binary black hole explorer

Visualization of precessing binary black holes

[Varma, Stein, Gerosa, 1811.06552]



Binary black hole explorer

Visualization of precessing binary black holes

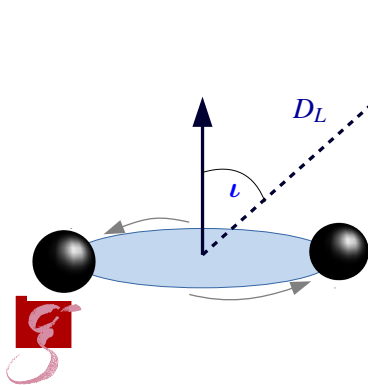


Binary black hole explorer

Visualization of precessing binary black holes

Distance and inclination

$$h_+ \approx 2(1 + \cos^2 \iota) \frac{M\eta v_{\text{orb}}(t)^2}{D_L} \cos [2\phi_{\text{orb}}(t)]$$



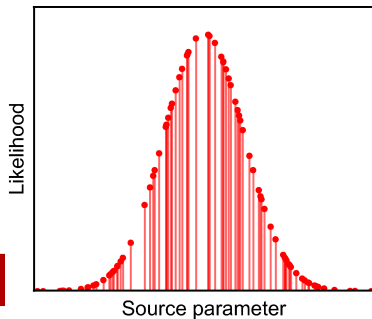
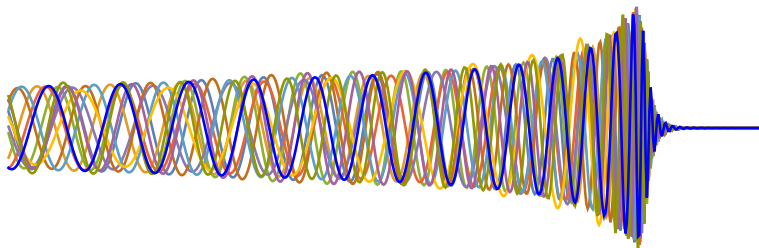
LIGO

M : total mass, $M = m_1 + m_2$

η : symmetric mass ratio,
 $\eta = m_1 m_2 / M^2$

v_{orb} : orbital velocity

ϕ_{orb} : orbital phase

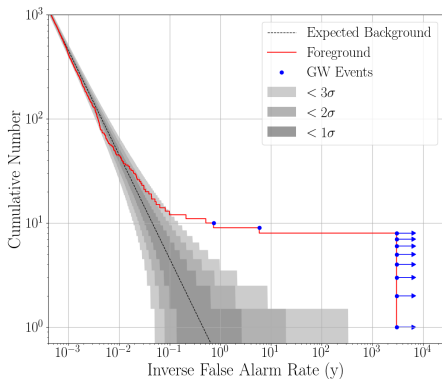


- ϑ : Source parameters
- $\Lambda(s|\vartheta) \sim \exp(-\frac{1}{2}\|s - h(\vartheta)\|^2)$
- **Posterior probability** ($\vartheta|s$)
 $\sim \Lambda(s|\vartheta) \times \text{prior}(\vartheta)$



GWTC-1

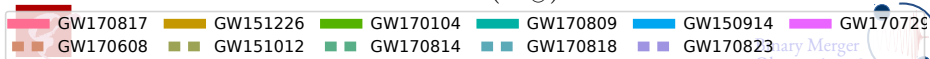
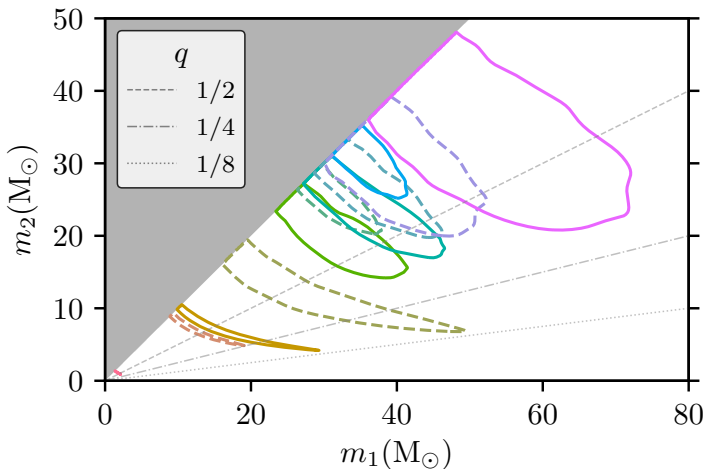
Gravitational-Wave Transient Catalog

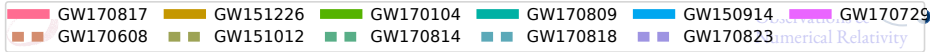
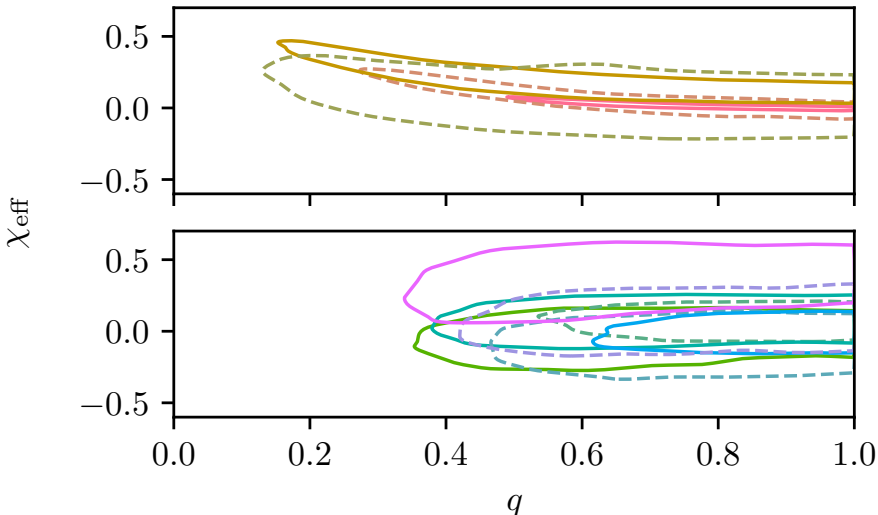


- Advanced LIGO's first and second observing runs, 2015-2017
- 10 binary black holes
- 1 binary neutron star

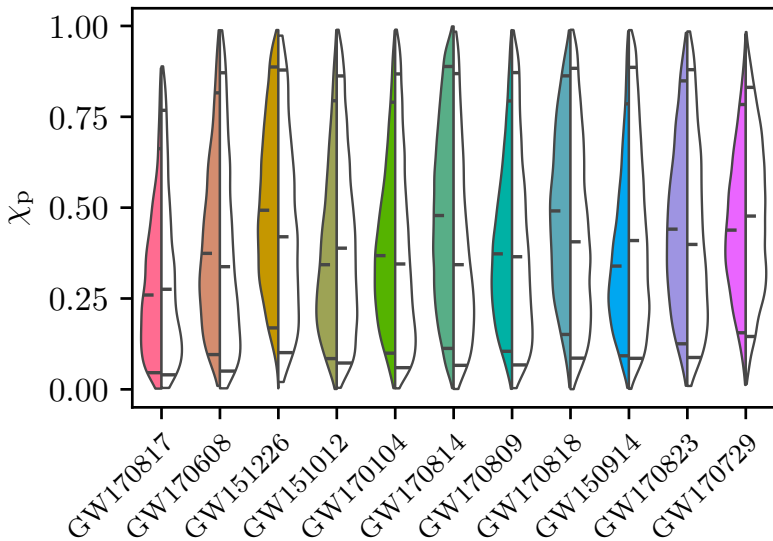
[LIGO+Virgo 1811.12907]







GWTC-1





GW150914



GW151012



GW151226



GW170104



GW170608



GW170729



GW170809



GW170814

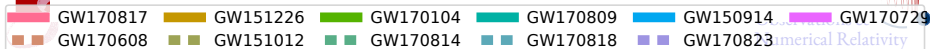
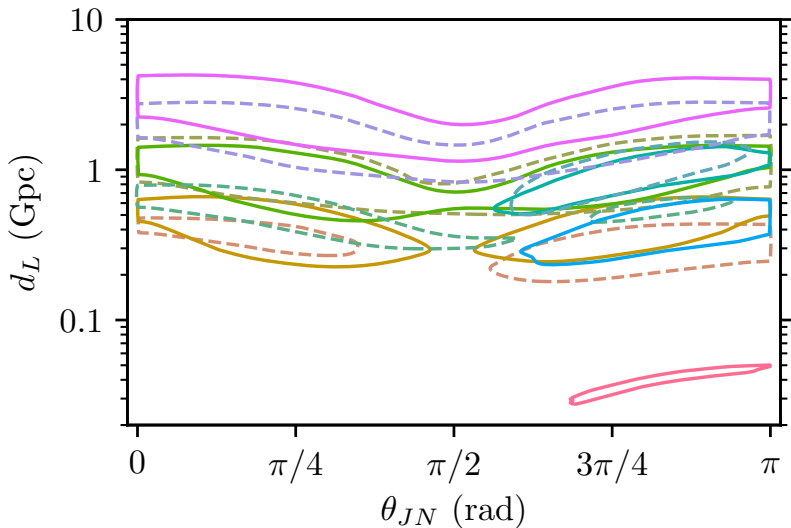


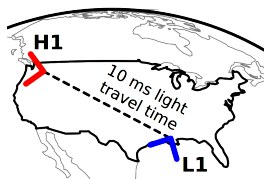
GW170818



GW170823

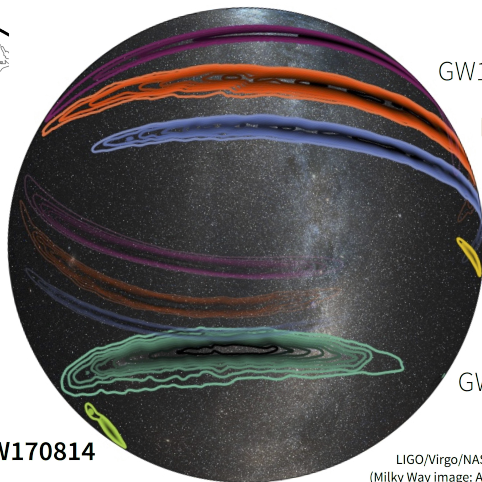






$$h = F_+(\alpha, \delta, \psi) h_+ + F_\times(\alpha, \delta, \psi) h_\times$$

GW170814



GW170104

LVT151012

GW151226

GW170817

GW150914



LIGO/Virgo/NASA/Leo Singer
(Milky Way image: Axel Mellinger)

Binary Merger
Observations &
Numerical Relativity



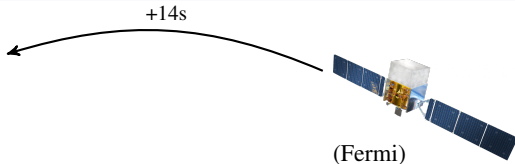
GW170817

August 17, 2017 – first binary neutron star detection

[ApJL 848:L12 (2017)]

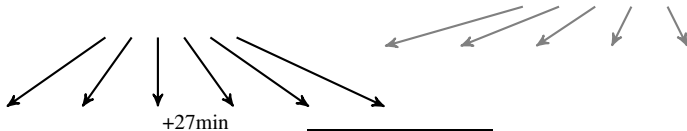


(LIGO)

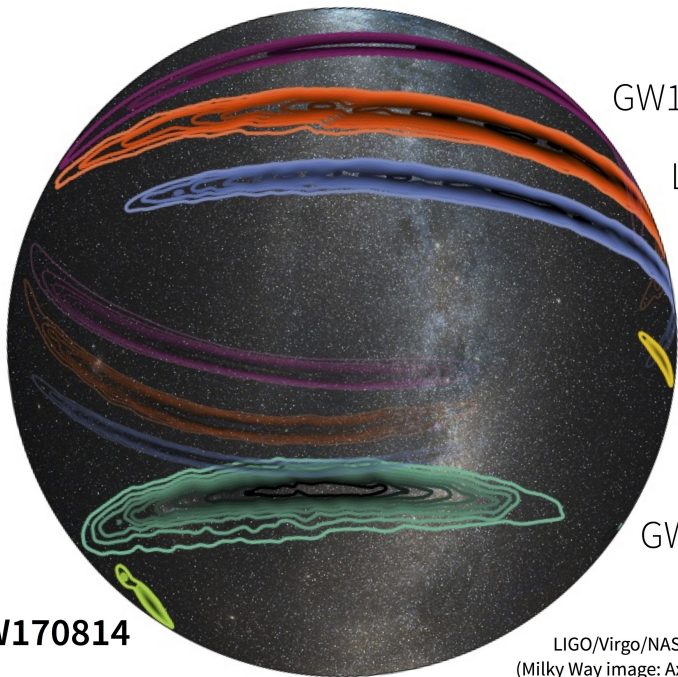


Wait...

12:41:06 UTC: I've seen a γ -ray burst.



GW170814



GW170104

LVT151012

GW151226

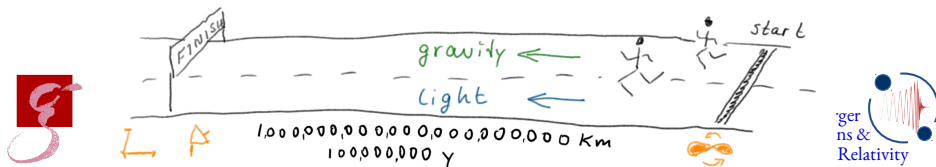
GW170817

GW150914

LIGO/Virgo/NASA/Leo Singer
(Milky Way image: Axel Mellinger)

Highlight results

- Binary neutron-star mergers occur and are measurable through gravitational waves. [LIGO/Virgo, PRL119 no.16 161101 (2017)]
- Binary neutron-star mergers are progenitors of short gamma-ray bursts and kilonovae. [LIGO/Virgo/Fermi, ApJL 848, L13 (2017)]
- A significant fraction of heavy elements (gold, platinum, etc. . .) is created in neutron-star mergers.
- Matter at extreme densities is not very stiff.
- The speed of light and speed of gravity are similar to at least $\Delta v/c \lesssim 10^{-15}$.





Gravitational Wave Open Science Center

Getting Started

Data

Catalogs

Bulk Data

Tutorials

Software

Detector Status

Timelines

My Sources

GPS ↔ UTC

About the detectors

Projects

Acknowledge
GWOSC

www.gw-openscience.org



LIGO Hanford Observatory, Washington
(Credits: C. Gray)



LIGO Livingston Observatory, Louisiana
(Credits: J. Glanville)

The Gravitational Wave Open Science Center provides data from [gravitational-wave](#)

NEW [O2 Bulk Data Release!](#)

 [Get started!](#)

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 [GWTC-1: Catalog of Compact Binary Mergers](#)

 [Join the email list](#)

 [Attend an open data workshop](#)





Primer on public alerts for astronomers from the LIGO and Virgo gravitational-wave observatories.

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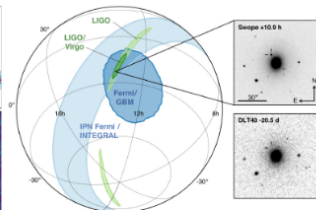
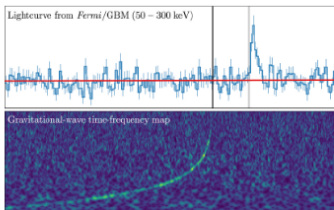
Email emfollow-userguide@support.ligo.org

[Quick search](#)

<https://emfollow.docs.ligo.org/userguide/>

[Getting Started Checklist](#) →

LIGO/Virgo Public Alerts User Guide



Welcome to the LIGO/Virgo Public Alerts User Guide! This document is intended for both professional astronomers and science enthusiasts who are interested in receiving alerts and real-time data products related to gravitational-wave (GW) events.


Warning:

Some technical details of LIGO/Virgo public alerts may change before the start of Observing Run 3 (O3) in 2019. In particular, details of the alert format and

Numerical Relativity

What I intended you learn

- **Basics of gravitational-wave emission**
 - Source: second time derivative of mass quadrupole moment
- **Gravitational-wave interferometers**
 - GW \rightarrow differential length change \rightarrow laser light phase difference \rightarrow signal
 - Complex instruments, variety of noise sources
- **Gravitational-wave analysis**
 - If model available: extract information by comparing data and model
- **Binary dynamics and measurement**
 - Masses & spins \leftrightarrow phase/frequency evolution
 - Distance & inclination \leftrightarrow amplitude
 - Location \leftrightarrow time difference

 Gravitational-wave astronomy in action